

# Nature of the chemical bond and prediction of radiation tolerance in pyrochlore and defect fluorite compounds

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## Abstract

The radiation tolerance of synthetic pyrochlore and defect fluorite compounds has been studied using ion irradiation. We show that the results can be quantified in terms of the critical temperature for amorphization, structural parameters, classical Pauling electronegativity difference, and disorder energies. Our results demonstrate that radiation tolerance is correlated with a change in the structure from pyrochlore to defect fluorite, a smaller unit cell dimension, and lower cation–anion disorder energy. Radiation tolerance is promoted by an increase in the Pauling cation–anion electronegativity difference or, in other words, an increase in the ionicity of the chemical bonds. A further analysis of the data indicates that, of the two possible cation sites in ideal pyrochlore, the smaller *B*-site cation appears to play the major role in bonding. This result is supported by *ab initio* calculations of the structure and bonding, showing a correlation between the Mulliken overlap populations of the *B*-site cation and the critical temperature.

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## 1. Introduction

Pyrochlore is important in nature as an ore mineral (Nb and Ta) and as a carrier of lanthanide and actinide (Th and U) elements in the Earth's crust. The structure type exhibits a range of useful properties for materials science applications including ionic conductivity (both cations and anions), electrical conductivity, and magnetic properties [1–3]. Pyrochlore is also one of the principal actinide host phases in oxide ceramics designed for the safe disposal of actinide-rich wastes derived from nuclear power generation and the nuclear weapons programs [4–6]. The pyrochlore structure type also has a high tolerance for impurities, is capable of very high waste loadings, and shows excellent chemical durability in aqueous fluids [7–9].

One major concern for these structure types is that they will undergo a crystalline to amorphous transformation as a function of the cumulative alpha decay dose over time. This may lead to volume expansion, cracking, and reduced chemical durability of the waste form. Radiation damage in these materials has been studied using samples doped with short-lived <sup>238</sup>Pu (half-life = 87 years) or <sup>244</sup>Cm (half-life = 18 years) [10–12], natural samples [13–15], and ion irradiation techniques [16–24]. Although actinide doping experiments are the most relevant to real waste forms, the experiments are difficult, expensive, and limited in scope. Studies of natural pyrochlores also provide complementary information on the long-term behavior in geological environments, but in many cases it is difficult to determine the time–temperature history. In recent years, a number of investigators have chosen to simulate the damage produced by alpha decay processes using ion irradiation techniques, especially the *in situ* ion irradiation method using thin transmission electron microscope (TEM) specimens.

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The ion irradiation studies noted above have identified some of the trends of composition and structure with respect to the critical amorphization dose ( $D_c$ ) and the critical temperature ( $T_c$ ), above which the material remains crystalline. Results of these studies reveal increasing radiation tolerance (decreasing  $T_c$ ) as the pyrochlore structure becomes more fluorite-like [25–29]. It should be noted that the structural data and  $A$ – $B$  cation radius ratios ( $R_A/R_B$ ) are not sufficient to explain all of the observed differences in radiation tolerance [30]. In this paper, we illustrate the relationships between  $T_c$  and various structural, bonding, and energy parameters. These relationships are presented in the form of empirical equations for the prediction of the critical temperature of pyrochlore and defect fluorite compounds (Fig. 1).

## 2. Crystal structure of pyrochlore

The pyrochlore structure is a superstructure of the fluorite ( $MX_2$ ) structure, and is based upon a  $2 \times 2 \times 2$  supercell containing  $M_4O_8$ , with ordered vacancies in the oxide anionic lattice. The space-group symmetry of pyrochlore is  $Fd\bar{3}m$  (no. 227), while that of the parent fluorite structure is  $Fm\bar{3}m$  (no. 225). The structural formula of ideal, stoichiometric pyrochlore can be written as  $^{VIII}A_2^{VI}B_2^{IV}X_6^{IV}Y$  in which  $A$  and  $B$  represent cations,  $X$  and  $Y$  represent anions, and the Roman numeral superscripts refer to their coordination numbers. In detail, the local coordination environments of each site are  $AX_6Y_2$ ,  $BX_6$ ,  $XA_2B_2$ , and  $YA_4$  [31,32].

The  $A$  cation is located on  $16c$  (000) and the  $B$  cation is located on  $16d$  ( $\frac{1}{2}\frac{1}{2}\frac{1}{2}$ ) in origin choice 2 (at center of symmetry) of space group  $Fd\bar{3}m$ . There are three crystallographically distinct anion sites in the pyrochlore lattice, these are the  $48f$  ( $x\frac{1}{8}\frac{1}{8}$ ),  $8a$  ( $\frac{1}{8}\frac{1}{8}\frac{1}{8}$ ), and  $8b$  ( $\frac{3}{8}\frac{3}{8}\frac{3}{8}$ ) sites. In ideal pyrochlore, the oxygen atoms are ordered onto  $48f$  and  $8a$  sites and the  $8b$  site is vacant, allowing the adjacent  $48f$  anions to relax toward the vacant site. This results in the value of the  $x48f$  coordinate changing from 0.375 in the ideal fluorite structure to values near 0.33 for a large number of oxide pyrochlores. With increasing  $R_A/R_B$ , generally above values of 1.78, certain pyrochlores are found to possess the defect fluorite structure. This is the

result of disordering of the  $A$  and  $B$  cations and disordering of the anions to give occupancies of 0.875 on the  $48f$ ,  $8a$ , and  $8b$  sites. In pyrochlore solid-solutions with  $R_A/R_B$  approaching 1.78, this disordering process may be continuous (albeit non-linear) and is accompanied by a change in  $x48f$  toward 0.375. Thus, many of these pyrochlores are partially disordered [1].

## 3. Experimental data and statistical analysis

The data discussed in this paper have been obtained by a number of investigators primarily for pyrochlores with  $A = Y$  and lanthanides and  $B = Ti, Sn, Zr,$  and  $Hf$  [17–31]. Experiments were conducted using in situ irradiation of thin TEM samples using 1.0 MeV Kr or in certain cases 1.5 MeV Kr ions at the IVEM-Accelerator Facility, Argonne National Laboratory, USA [33]. Fig. 2 shows the critical temperatures of pyrochlore compounds plotted against the cation–anion radius ratio ( $R_M/R_X$ ), where  $M$  represents the average radius of the  $A$  and  $B$  cations.

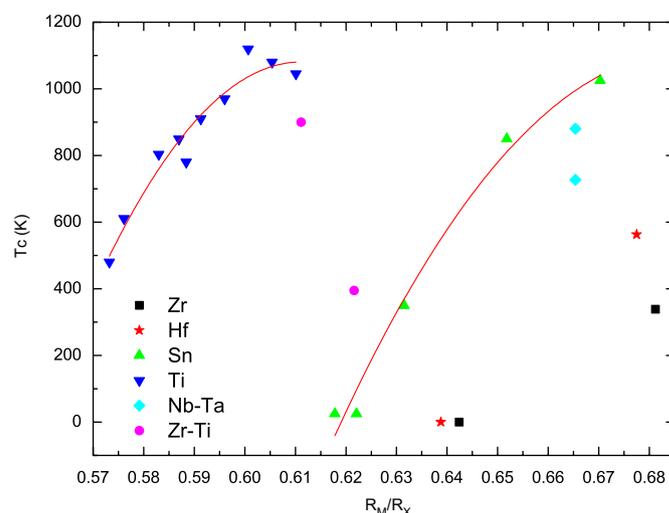


Fig. 2. Plot of the average metal cation ( $M$ ) to anion radius ratio ( $R_M/R_X$ ) versus the critical amorphization temperature ( $T_c$ ) for 21 III–IV pyrochlore compounds plus two natural pyrochlores  $NaCaNb_2O_6F$  and  $NaCaTa_2O_6F$  (diamonds). The  $Ln_2Ti_2O_7$  and  $Ln_2Sn_2O_7$  series are delineated by the curves.

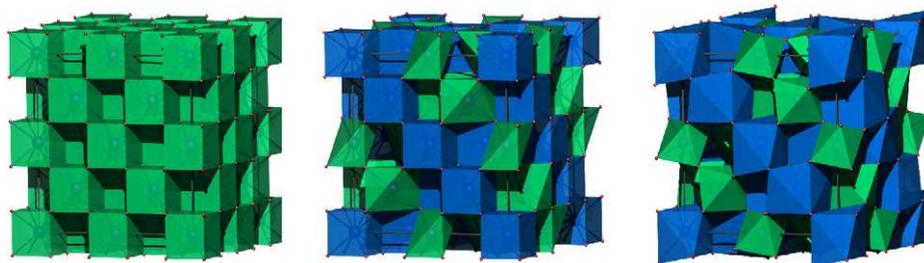


Fig. 1. Crystal structures of fluorite, ordered defect fluorite, and pyrochlore. The fluorite structure shows the cubic nature of the anion coordination around the disordered cations. The defect fluorite shows the effect of removing the  $8a$  anion from the lattice, with  $x(48f)$  remaining at 0.375, with the eight coordinated  $A$ -site shown in blue and the six coordinated  $B$ -site shown in green. The pyrochlore structure shows the effect of the  $48f$  relaxation from 0.375 to 0.3125. The spheres in all structures show the location of the oxygen anions in the lattice.

This is a convenient method of plotting as the data sets are well separated and are related to structural stability according to Pauling's rules (e.g., increased cation coordination and phase transformation is favored by increasing  $R_M/R_X$  values). All of the lanthanide titanate pyrochlores shown in Fig. 2 can be amorphized with critical temperatures above about 450 K. The radiation response appears to be non-linear and may roll over at the cubic–monoclinic phase transformation which occurs between  $\text{Sm}_2\text{Ti}_2\text{O}_7$  and  $\text{Nd}_2\text{Ti}_2\text{O}_7$ . Data for lanthanide stannate pyrochlores also appear to exhibit non-linear behavior; however, in this case the compounds with lanthanides heavier than Dy–Ho are resistant to amorphization. The hafnate and zirconate pyrochlores with lanthanides heavier than Gd are radiation resistant.

Multiple linear regression methods were used to conduct a statistical analysis of the critical temperature for 19 different pyrochlore and defect fluorite compounds, in this instance with  $T_c$  as the dependent variable. The  $X$ -anion coordinate ( $x48f$ ), unit cell edge ( $a_0$ ),  $A$ – $B$  cation radius ratio ( $R_A/R_B$ ), cation–anion radius ratio ( $R_M/R_X$ ), average anion–cation Pauling electronegativity difference ( $\Delta X_p$ ), and combined cation–anion disorder energy ( $E_{\text{dis}}$ ) were used as the independent variables. Values for the latter were obtained from the *ab initio* calculations of Grimes and co-workers [32,33]. In this work, we have used the  $x48f$  scale ranging from 0.3125 for perfect pyrochlore to 0.375 for defect fluorite. Among these variables both simple negative and positive correlations are observed between  $T_c$  and  $x48f$  and  $T_c$  and  $R_A/R_B$ , respectively. These relationships have been recently discussed in the literature [26,30]. More complex correlations are observed for  $T_c$  and the other independent variables  $a_0$ ,  $R_M/R_X$ ,  $\Delta X_p$ , and  $E_{\text{dis}}$ . Note that the useful combinations of independent variables are limited due to high statistical correlations between certain pairs of variables (e.g.,  $R = 0.99$  for  $a_0$  and  $R_M/R_X$ ,  $R = 0.92$  for  $R_A/R_B$  and  $E_{\text{dis}}$ ). The best statistical model derived from these data relates the critical temperature to the following structural, bonding, and energy parameters:

$$T_c = -29738.6(x48f) + 8457.7(a_0) - 1148.9(\Delta X_p) + 939.7(E_{\text{dis}}). \quad (1)$$

The model shown above is highly significant with  $R^2 = 0.991$  and a standard deviation of 82 K for the predicted value of the critical temperature. Furthermore, all of the independent variables are highly significant as shown by the magnitude of the Student's  $t$ -test, which lies between 5 and 15 for these four parameters. A plot (not shown) of the calculated versus observed critical temperatures for the pyrochlore and defect fluorite compounds used in the model indicates that there is excellent agreement between the model and observed  $T_c$  values across the observed temperature range. This plot also shows that the critical temperatures [21] of the natural pyrochlores  $\text{NaCaNb}_2\text{O}_6\text{F}$  and  $\text{NaCaTa}_2\text{O}_6\text{F}$  are predicted to within 60 and 150 K, respectively, suggesting that this or a similar

model might be applicable to pyrochlore compounds in general.

In order to further investigate the effects of bonding, we performed multiple regression analyses using the individual electronegativities of the  $A$  and  $B$  cations,  $X_{pA}$  and  $X_{pB}$ , instead of the average cation–anion electronegativity difference. Retaining the same set of independent variables used in the development of Eq. (1), the best model that we obtained is as follows:

$$T_c = -33218.6(x48f) + 6722.9(a_0) + 571.8(X_{pB}) + 866.3(E_{\text{dis}}). \quad (2)$$

This model includes the same structural and energy terms as in Eq. (1) and also returns a similar level of statistical significance, with  $R^2 = 0.991$ , a standard deviation of 81 K for the predicted value of the critical temperature, and robust Student's  $t$  values. Notice that the sign of the electronegativity term in Eq. (2) is now positive. This is because we have used the electronegativity of the cation itself instead of the difference in electronegativities between the cation and anion. Inclusion of  $X_{pA}$  in the equation does not significantly improve the regression statistics. This parameter was rejected on the basis of the  $t$  value of 1.06. Therefore, it appears from this analysis that the electronegativity of the  $B$  cation has the most significant correlation with radiation tolerance.

Using the empirical model represented by Eq. (1) and structural data for 51 different compositions, we have determined the  $T_c$  response surface for III–IV pyrochlores as a function of the ionic radii of the  $A$  cation ( $Y$  and lanthanides) and  $B$  cation ( $\text{Ti}$ ,  $\text{Mo}$ ,  $\text{Sn}$ ,  $\text{Hf}$ ,  $\text{Zr}$ ). Fig. 3 is a two-dimensional contour map of the predicted critical temperature, illustrating that the response surface is a

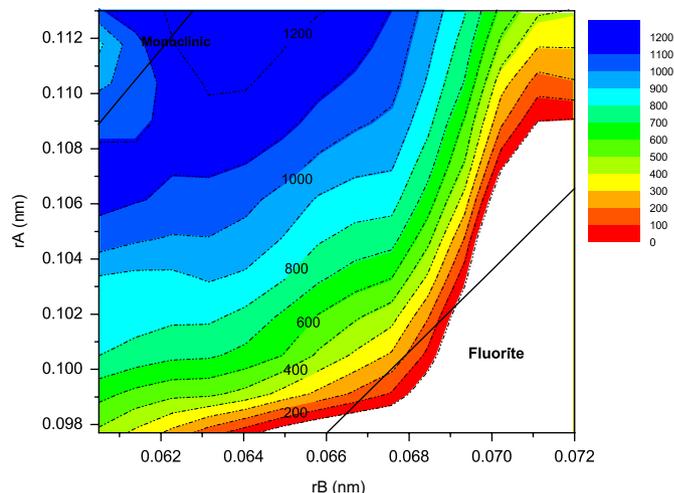


Fig. 3. Contour map of the predicted critical amorphization temperature for III–IV pyrochlore compounds versus the  $A$ -site and  $B$ -site cation radii. Contours of  $T_c$  are shown in degrees Kelvin. This figure was constructed using data for pyrochlores with  $A = \text{La–Lu}$  plus  $Y$  and  $B = \text{Ti, Mo, Sn, Hf, and Zr}$ . The range of pyrochlore stability are shown and labeled as monoclinic and fluorite.

complex function of the material properties in this region of the III–IV pyrochlore composition space. Notice that the  $T_c$  contours curve upwards toward the right side of the figure in the vicinity of the larger  $B$  cations. This curvature reflects the increasing radiation resistance of pyrochlore and defect fluorite compounds with increasing  $B$  cation size (e.g., Sn, Hf, and Zr).

The three-dimensional form of the radiation response surface is shown in Fig. 4. Here, we see that the surface rises steeply from 0 K and then levels off at high temperatures for the compositions with large  $A$ -site and small  $B$ -site cation radii. The form of the surface shown in Fig. 4 also reflects, to a certain extent, the non-linear trends of the Ti and Sn data sets plotted in Fig. 2. Based upon this curvature, we suggest that the  $T_c$  values of the  $\text{Ln}_2\text{Ti}_2\text{O}_7$  compounds may begin to decrease beyond the cubic–monoclinic phase transition within the stability field of the monoclinic layered perovskites with  $\text{Ln} = \text{Nd}, \text{Pr}, \text{Ce},$  and  $\text{La}$ .

#### 4. *Ab initio* calculations

We carried out first principles calculations of the structures of selected pyrochlore and defect fluorite compounds with  $A = \text{Y}, \text{La}$  and  $B = \text{Ti}, \text{Zr}, \text{Sn}, \text{Hf}$ . These calculations were performed using SIESTA, a self-consistent implementation of density functional theory in combination with the pseudo-potential approximation to remove core electrons from consideration [34]. From these data, we have calculated the Mulliken overlap populations as a measure of the A–O and B–O bonds (Table 1).

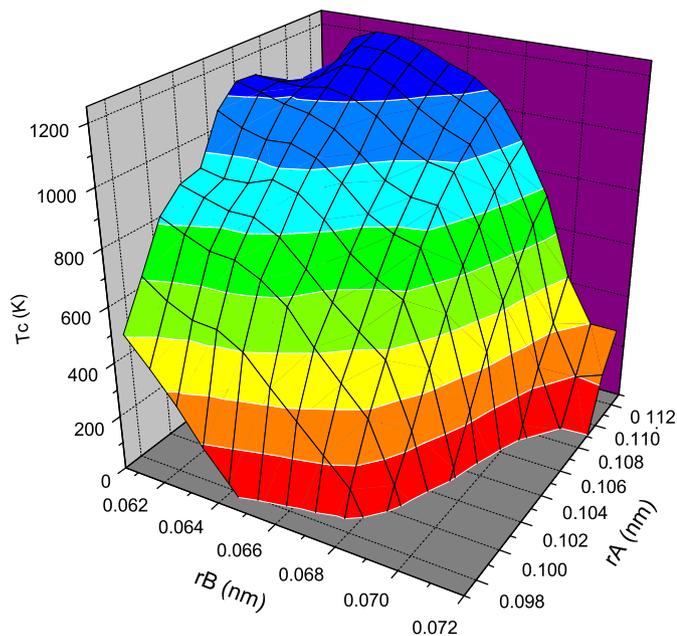


Fig. 4. Three-dimensional representation of the predicted critical amorphization temperature. This figure shows the approximate form of the surface and suggests that the critical temperature levels off, possibly decreasing in the field of the monoclinic structure types with  $A = \text{Nd}–\text{La}$ .

Mulliken overlap populations are frequently used as a measure of ionicity/covalency, where greater overlap (larger numerical value in Table 1) indicates increased covalency.

In general, the results are reasonable given the uncertainties involved in the calculations for these relatively complex oxides. Although the calculated value of the Mulliken overlap population for Hf seems high relative to Zr, the result does provide an explanation for the large difference in  $T_c$  between  $\text{La}_2\text{Zr}_2\text{O}_7$  (339 K) and  $\text{La}_2\text{Hf}_2\text{O}_7$  (563 K) given that the structures of these two pyrochlores are nearly identical [35].

For the La compounds listed in Table 1, the data show that the ionicity of the B–O bonds increases in the order  $\text{Sn} < \text{Hf} < \text{Zr}$  (note that  $\text{La}_2\text{Ti}_2\text{O}_7$  is not a pyrochlore, it is a layered perovskite structure type similar to  $\text{Ca}_2\text{Nb}_2\text{O}_7$ ). In comparison, the Pauling electronegativity data indicate that the ionicity should increase in the order  $\text{Sn} < \text{Zr} < \text{Hf}$ , although the individual electronegativities of Zr (1.33) and Hf (1.30) are quite close to one another. This is not an unusual result, as the electronegativity scales are very general and cannot be expected to predict the detailed behavior of different compounds in every case. Nevertheless, the results presented here suggest that bonding effects are dominant for the La compounds, as there are only minor differences in the  $X$ -anion coordinate and disorder energies (see Table 1).

Table 1 also shows that Y and La have a similar level of ionicity ( $M_{A-O} = 0.026–0.041$ ) in all eight compounds, with the Y–O bonds being consistently slightly more ionic than the La–O bonds. This is an important result, since the structure of pyrochlore can also be viewed as two interpenetrating networks, a  $B_2X_6$  octahedral framework with hexagonal tungsten bronze-type layers on (111) planes and an anti-cristobalite type  $A_2Y$  network [32]. Thus, it appears that the nature of the bonding of the  $B_2X_6$  framework exerts a major control on radiation tolerance in these compounds. This result is in agreement with the empirical model of Eq. (2). Upon examination of the data for the Y compounds, we note that  $\text{Y}_2\text{Ti}_2\text{O}_7$  does not fit the picture derived from the Mulliken overlap populations alone. Further examination of Table 1 shows the structural and disorder energy parameters which show much larger differences for these four compounds. In particular,  $\text{Y}_2\text{Ti}_2\text{O}_7$  has the lowest  $X$ -anion coordinate (more pyrochlore-like) and the highest disorder energy, suggesting that these parameters are dominant over bonding effects. This is consistent with the form of the  $T_c$  surface shown in Figs. 3 and 4.

#### 5. Discussion and conclusions

This study shows that radiation damage data can be statistically quantified as a function of structural, bonding, and disorder energy parameters. Furthermore, based upon the available data for two natural pyrochlore samples, we show that the statistical approach may be generally

Table 1  
Mulliken overlap populations ( $M$ ) for  $A$ -O and  $B$ -O bonds of pyrochlore compounds with  $A = Y, La$  and  $B = Ti, Zr, Sn$ , and  $Hf$

Compound	$M_{A-O}$	$M_{B-O}$	$\Delta X_p (A)$	$\Delta X_p (B)$	$x48f$	$E_{dis}$ (eV)	$T_c$ (K) observed
$Y_2Sn_2O_7$	0.026	0.202	1.22	1.96	0.337	3.6	—
$Y_2Ti_2O_7$	0.027	0.111	1.22	1.54	0.330	4.8	780
$Y_2Hf_2O_7$	0.029	0.090	1.22	1.30	0.375	3.0	—
$Y_2Zr_2O_7$	0.026	0.017	1.22	1.33	0.375	2.8	—
$La_2Sn_2O_7$	0.034	0.207	1.10	1.96	0.329	4.2	1025
$La_2Ti_2O_7$	0.036	0.110	1.10	1.54	—	—	—
$La_2Hf_2O_7$	0.041	0.096	1.10	1.30	0.331	4.1	563
$La_2Zr_2O_7$	0.037	0.027	1.10	1.33	0.332	4.0	339

Larger values of the overlap population are related to increased covalency, e.g., sharing of electrons via overlapping atomic orbitals between atoms.

applicable to stoichiometric pyrochlores with a range of  $A$ -site and  $B$ -site cation valence combinations. The statistical analysis given above indicates that structural aspects are important contributors to radiation tolerance. In the case of the pyrochlore structure, the topological element ( $x48f$  parameter) describes the change from pyrochlore-like to fluorite-like geometry. It is well known that this topological change is associated with increased oxygen ion conductivity [1], a factor that may contribute to enhanced defect mobility and recombination in thin films during ion irradiation. This is particularly true of the materials studied in this paper, whereby ionic conductivity may be enhanced by several orders of magnitude upon the development of anion disorder over the  $48f$ ,  $8a$ , and (normally vacant)  $8b$  sites.

Radiation tolerance and structural aspects are also related to the concept of structural freedom,  $f$ , and its relationship to topological disorder as discussed by Hobbs et al. [36]. In this concept the characteristic structural units are the coordination polyhedra each having  $V$  vertices and the connectivity,  $C$ , is defined as the average number of polyhedra sharing each vertex. The latter can be further described by the relative proportions of edges and faces shared with other polyhedra. Effectively, the structural freedom is the difference between the degrees of freedom given by the structure dimensionality and the number of constraints imposed by the connectivity. This is represented by the equation below, in which  $d$  is the dimensionality of the structure,  $\delta$  is the dimensionality of the polyhedron (or “polytope”),  $Y$  is the fraction of edge-sharing vertices, and  $Z$  is the fraction of vertices sharing faces with  $p$  sides:

$$f = d - C \left\{ \delta - \left[ \frac{\delta(\delta + 1)}{2V} \right] \right\} - (d - 1) \left( \frac{Y}{2} \right) - [(p - 1)d - (2p - 3)] \left( \frac{Z}{p} \right).$$

In the case of pyrochlore-defect fluorite compounds (and many other structures types), the topological degrees of freedom may be calculated from the entire structure or from the major structural elements, e.g., the  $B_2X_6$  framework or  $A_2Y$  network. In ideal fluorite, the structural freedom derived from the whole structure is  $-7.0$ . In the

case of pyrochlore, the value of  $f = -6.1$  for the whole structure, whereas the  $B_2X_6$  and  $A_2Y$  networks give values of  $-1.0$  and  $0.0$ , respectively. If one or the other of these networks exerts a dominant effect on the properties of the crystal, then the “apparent”  $f$  value might be considerably greater than that calculated for the whole structure. It has been suggested previously that the  $B_2X_6$  framework is the main structural element and this is in accord with the range of known defect pyrochlores. Furthermore, the *ab initio* calculations suggest that the  $A_2Y$  network is generally ionic in nature (low Mulliken overlap population) whereas the bonding of the  $B_2X_6$  framework changes according to the nature of the  $B$ -site cation. These results indicate, everything else being equal, that the radiation tolerance follows the order fluorite > defect fluorite > pyrochlore. This is in general agreement with the data for the  $X$ -anion coordinate and disorder energies.

The empirical models described in this paper also demonstrate that electronegativity (and therefore ionicity) is an important parameter, particularly in the case of the  $B$ -site cation. This result confirms the bond-type criterion proposed by Naguib and Kelly [37], who showed a broad correlation between electronegativity and radiation tolerance. A recent review of radiation damage effects in oxide pyrochlores by Ewing and co-workers [38] has further illustrated the importance of electronic structure and bonding through comparison of different compositions (e.g.,  $Gd_2Sn_2O_7$  and  $Gd_2Hf_2O_7$ ) with otherwise similar properties such as the  $A$ - $B$  cation radius ratio. Trachenko [39] has given a more general review of the physics of radiation damage where it is suggested that short-range covalent and long-range ionic contributions to the total force field between any given pair of atoms interact to produce a “landscape” of potential energy. The full three-dimensional expression of this landscape, with its various energy minima (and activation barriers) in a crystal determines the ability to recover the disorder produced by an atomic collision cascade. In general, short-range covalent contributions lead to highly directional bonds (e.g., orbital hybridization, polyhedral distortion) and a number of distinct potential energy minima which act as barriers to recovery of periodicity in the vicinity of the collision cascade. Long-range ionic contributions tend to

simplify the energy landscape, thereby minimizing the barriers to recovery of atomic periodicity. The empirical models and *ab initio* calculations discussed in the present work both support the role of ionicity in promoting radiation tolerance in pyrochlore compounds.

The positive correlation between  $T_c$  and the combined cation–anion disorder energy is consistent with the contour plots reported in the literature [32,33]. These calculations indicate that  $E_{\text{dis}}$  decreases with decreasing A-site cation radius and increasing B-site cation radius, where radiation tolerant defect fluorite structures are encountered in the III–IV pyrochlore composition space. Comparison of Figs. 3 and 5 in Minervini et al. [32] show that the degree of correlation between the critical temperature and the disorder energy increases for the larger B-site cations. When examined in detail, we see that the contour lines of the disorder energy are nearly vertical for the smaller B-site cations. Thus, the disorder energy appears to play a more important role in promoting radiation resistance with increasing B-site cation radius in this system.

In conclusion, the radiation tolerance of pyrochlore and defect fluorite compounds can be described by a combination of structural, bonding, and energetic parameters. The results of this study apply strictly to thin crystals of these materials irradiated with 1.0–1.5 MeV Kr ions, as the radiation response is known to vary as a function of ion mass, energy, and in some cases ion flux (e.g., the rate of ions hitting the sample) [38,40]. For the compounds considered in this work, the effects of ion mass and energy remain to be examined in detail. The challenge ahead is to understand these relationships in greater detail, both within the field of a given structure type and across the phase boundaries into the fields of neighboring compounds. In order to accomplish the latter part of this task, a set of universal structural parameters (e.g., volume and structural distortion) must be found.

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