

Atomic physics and quantum optics using superconducting circuits

J. Q. You^{1,2} & Franco Nori^{2,3}

Superconducting circuits based on Josephson junctions exhibit macroscopic quantum coherence and can behave like artificial atoms. Recent technological advances have made it possible to implement atomic-physics and quantum-optics experiments on a chip using these artificial atoms. This Review presents a brief overview of the progress achieved so far in this rapidly advancing field. We not only discuss phenomena analogous to those in atomic physics and quantum optics with natural atoms, but also highlight those not occurring in natural atoms. In addition, we summarize several prospective directions in this emerging interdisciplinary field.

Superconducting circuits with Josephson junctions can behave as artificial atoms. In these quantum circuits, the Josephson junctions act as nonlinear circuit elements (Box 1). Such nonlinearity in a circuit ensures an unequal spacing between energy levels, so that the lowest levels can be individually addressed by using external fields (see, for example, refs 1–9). Experimentally, these circuits are fabricated on a micrometre scale and operated at millikelvin temperatures. Because of

the reduced dimensionality and thanks to the superconductivity, the environment-induced dissipation and noise are greatly suppressed, so the circuits can behave quantum mechanically.

Superconducting circuits based on Josephson junctions have recently become subjects of intense research because they can be used as qubits—controllable quantum two-level systems—for quantum computing (see, for example, refs 1–4 for reviews). Even though the typical decoherence times of these circuits fall short of the requirements for quantum computation, their macroscopic quantum coherence is sufficient for them to exhibit striking quantum behaviour. These circuits can have a number of superconducting eigenstates with discrete eigenvalues lower than the energy levels of the quasi-particle excitations that involve breaking Cooper pairs. This property allows these circuits to behave like superconducting artificial atoms. Indeed, there is a deep analogy between natural atoms and the artificial atoms made from superconducting circuits (Box 2). Both have discrete energy levels and can exhibit coherent quantum oscillations between these levels. Whereas natural atoms may be controlled using visible or microwave photons that excite electrons from one state to another, the artificial atoms in these circuits are driven by currents, voltages and microwave photons that excite the system from one macroscopic quantum state to another.

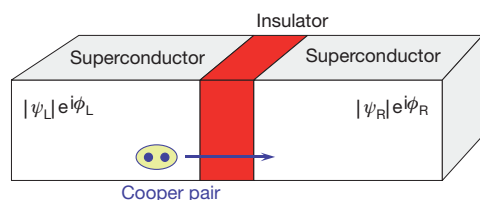
Differences between superconducting circuits and natural atoms include the different energy scales in the two systems, and how strongly each system couples to its environment; the coupling is weak for natural atoms and strong for circuits. In contrast to naturally occurring atoms, artificial atoms can be designed with specific characteristics and fabricated on a chip using standard lithographical technologies. With a view to applications, this degree of tunability is an important advantage over natural atoms. Thus, in a controllable manner, superconducting circuits can be used to test fundamental quantum mechanical principles at a macroscopic scale, as well as to demonstrate atomic physics and quantum optics on a chip. Moreover, these artificial atoms can be designed to have exotic properties that do not occur in natural atoms.

In this Review, we highlight the atomic-physics and quantum-optics phenomena found in superconducting circuits. The novel physics in these artificial atoms will be emphasized, including phenomena that do not occur in natural atoms. We also summarize several prospective directions in this emerging interdisciplinary field. Some of the examples in this brief overview relate to our work, because we are more familiar with them.

BOX 1

The Josephson junction as a nonlinear inductor

A superconductor contains many paired electrons, called Cooper pairs, which condense into the same macroscopic quantum state described by the wavefunction $|\psi|e^{i\phi}$, with $|\psi|^2$ being the density of Cooper pairs. In the absence of applied currents or magnetic fields, the phase ϕ is the same for all Cooper pairs. A Josephson junction is composed of two bulk superconductors separated by a thin insulating layer through which Cooper pairs can tunnel (see figure below). The supercurrent through the junction is $I = I_c \sin \phi$, where the critical current I_c is related to the Josephson coupling energy E_J of the junction by $I_c = (2e/\hbar)E_J$, and $\phi = \phi_L - \phi_R$ is the phase difference of the two superconductors across the junction. The time variation of this phase difference is related to the potential difference V between the two superconductors: $d\phi/dt = (2\pi/\Phi_0)V$, where $\Phi_0 = h/2e$ is the magnetic-flux quantum. From the definition of the inductance $V = L_J dI/dt$, it follows that $L_J = \Phi_0/(2\pi I_c \cos \phi)$, indicating that the Josephson junction behaves like a nonlinear inductor.

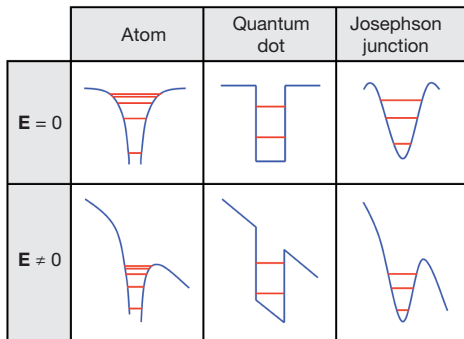


¹Department of Physics, State Key Laboratory of Surface Physics, Key Laboratory of Micro and Nano Photonic Structures (Ministry of Education), Fudan University, Shanghai 200433, China. ²Advanced Science Institute, RIKEN, Wako-shi 351-0198, Japan. ³Physics Department, The University of Michigan, Ann Arbor, Michigan 48109-1040, USA.

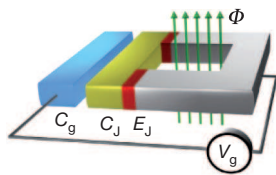
BOX 2

Artificial and natural atoms

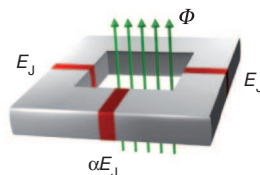
In the figure below, we show the potential energy (in blue) and discrete energy levels (in red) for an atom, a quantum dot (for example, a particle in a box) and a Josephson junction; these are shown in the absence ($E = 0$) and presence ($E \neq 0$) of an externally applied electric field. Owing to their confinement, the electrons in the atom and the quantum dot have discrete energy levels. The Cooper pairs confined in the potential well of the Josephson coupling energy also have discrete energy levels, and the junction can be regarded as a superconducting artificial atom.



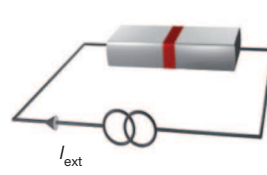
a Voltage-driven box (charge qubit)



b Flux-driven loop (flux qubit)



c Current-driven junction (phase qubit)



d Energy levels of the flux-driven loop

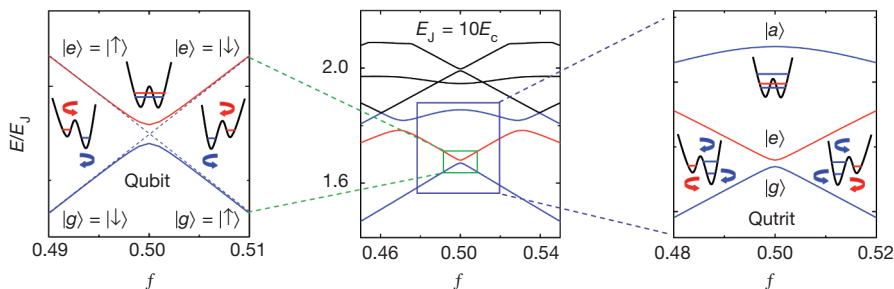


Figure 1 | Superconducting circuits as artificial atoms. **a**, A Cooper-pair box biased by a gate voltage V_g and implemented in the charge regime, $E_J/E_C \ll 1$. The SQUID loop provides an effective Josephson coupling energy tuned by the threading magnetic flux Φ . See main text for nomenclature. The blue, gold and grey components denote, respectively, a plate of the gate capacitor, a superconducting island acting as a 'box' of Cooper pairs, and a segment of a superconducting loop; each red component denotes the thin insulating layer of a Josephson junction. **b**, A superconducting loop interrupted by three Josephson junctions and implemented in the phase regime, $E_J/E_C \gg 1$. The two identical Josephson junctions have coupling energy E_J and capacitance C , while both the Josephson coupling energy and the capacitance of the smaller junction are reduced by a factor α , where $0.5 < \alpha < 1$. The three-junction loop is biased by a flux Φ such that $f \equiv \Phi/\Phi_0 \approx \frac{1}{2}$. **c**, A Josephson junction biased by a current I_{ext} , which is also implemented in the phase regime and has a much larger ratio E_J/E_C . **d**, Energy levels of the flux-driven three-junction loop (blue, red and black curves in the middle panel). With the lowest two energy levels involved (blue and red curves in the left panel, which are enlarged from the smaller

Superconducting circuits as artificial atoms

Two important energy scales determine the quantum mechanical behaviour of a Josephson-junction circuit: namely, the Josephson coupling energy E_J and the electrostatic Coulomb energy $E_C = (2e)^2/2C$ for a single Cooper pair, where e is the electronic charge, and C is either the capacitance C_J of a Josephson junction or the capacitance of a superconducting island called a Cooper-pair box (namely, the sum of the gate capacitance C_g and the relevant junction capacitance), depending on the circuit. Figure 1 summarizes three kinds of superconducting circuits implemented in different regimes of E_J/E_C : Fig. 1a shows the voltage-driven box (also known as a Cooper-pair box) for a charge qubit⁵, Fig. 1b the flux-driven three-junction loop for a flux qubit⁶ and Fig. 1c the current-driven junction for a phase qubit^{8,9}. As a typical example, energy levels of the flux qubit are shown in Fig. 1d. Moreover, hybrid superconducting qubits are possible. For instance, a Cooper-pair box can behave like a charge-flux qubit⁷ when $E_J/E_C \approx 1$. As for the flux qubit, by reducing the ratio E_J/E_C , the charge noise can become dominant over the flux noise¹⁰ and the circuit then behaves more like a charge qubit. In this circuit, when $\alpha < 0.5$ (here α is the ratio of the Josephson coupling energy between the smaller and larger junctions in the loop), the double-well potential converts to a single-well potential and the circuit behaves like a phase qubit^{10,11}. One can shunt a large capacitance to the small junction^{10,11} to suppress the charge noise in this circuit. Also, this large capacitance shunted to the Josephson junction can be used to reduce the charge noise in the Cooper-pair box¹², so as to implement the circuit in the phase regime. Below we highlight several

rectangle in the middle panel), the flux-driven loop can behave like a coherent and controllable quantum two-level system (qubit), while the circuit can behave like a coherent and controllable three-level system (qutrit) when using the lowest three levels (blue and red curves in the right panel, which are enlarged from the larger rectangle in the middle panel). Moreover, in the left, top and right insets of the left (right) panel, the two (three) energy levels are also displayed in the double potential well for $f < \frac{1}{2}$, $f = \frac{1}{2}$ and $f > \frac{1}{2}$, where the clockwise and anticlockwise arrows (either blue or red) represent the circulating supercurrent states in the flux-driven three-junction loop. In **a–c**, the qubit employs the charge states on a single island, the persistent-current states in a double potential well, and the anharmonic-oscillator states in a single potential well, respectively. Also, a flux-driven superconducting loop with a different number of Josephson junctions, for example, one^{8,9} or four junctions⁹⁰, can be used for a flux qubit. Furthermore, a flux-driven single-junction loop can be used as a phase qubit when working with the energy levels in a tilted potential well⁹¹, as in a current-driven junction.

aspects of the atomic-physics and quantum-optics phenomena found in superconducting circuits.

Cavity quantum electrodynamics

A quantized electromagnetic field can coherently exchange energy with a two-level system, usually in a tiny (micrometre-scale) cavity. This energy exchange process involves a fundamental phenomenon called Rabi oscillation; the two-level system and the field exchange a quantum of energy back and forth at a characteristic frequency known as the Rabi frequency. When the field is in resonance with the system, the Rabi frequency is proportional to the system–field coupling strength. The most elementary of such coherent processes involves the interaction of a two-level system with a single photon in the cavity. The exchange of energy between the system and the single photon is observable when the Rabi frequency is larger than the decay rates of the two-level system and the cavity. This photon–atom coupling has been achieved for a variety of atoms interacting with the light field in a cavity, and forms the basis of cavity quantum electrodynamics (QED). Cavity QED with superconducting circuits was proposed^{13,14} and experimentally achieved^{15,16} in systems where superconducting qubits are employed as two-level artificial atoms. For the cavity, a single-mode inductance/capacitance (LC) resonator¹⁵ and a multi-mode coplanar waveguide resonator¹⁶ have been used. Significantly, the strong-coupling limit for a superconducting qubit in a cavity can be attained much more easily than for a natural atom in a cavity^{4,14} by suitably designing the system parameters. It allows, for example, the observation of the Lamb shift for a superconducting qubit in the cavity¹⁷. Moreover, both the superconducting qubit and the cavity can be fabricated on the same chip. For a review of cavity QED with superconducting qubits, see, for example, ref. 4.

Because they can be designed with specific system parameters, superconducting quantum circuits are suited for achieving the so-called ultrastrong-coupling regime, where the qubit–photon coupling strength is comparable to the energy scales of the qubit and the photon¹⁸. Indeed, there have been a number of theoretical studies of this system, analysing some of its rich static and dynamical properties (see, for example, refs 19–21). Also, the ultrastrong coupling between a superconducting flux qubit and a coplanar waveguide²² or an LC resonator²³ has recently been demonstrated in experiments. One can expect to find new phenomena in this ultrastrong-coupling regime that are not present in the conventional weak- and moderately strong-coupling regimes. In addition, dressed states of a superconducting charge qubit and an intense microwave field were experimentally observed by embedding the circuit in an LC oscillator²⁴. The tunability of these dressed states allows one to explore both resonant and dispersive coupling regimes.

Selecting quantum transitions

In natural atoms, the electronic state at each orbital level has a well-defined parity symmetry, either even or odd. Under the dipole approximation, the interaction Hamiltonian between the atom and the time-dependent electric field has odd parity. Thus, to have a non-zero dipole transition matrix element, there should be a parity change between the initial and final states, in addition to the constraints on azimuthal and magnetic quantum numbers of the electronic states. This optical selection rule dictates that only three types of three-level systems, called Λ -, V- and Ξ -type atoms (Fig. 2a), exist for the natural atoms, where no dipole transition between electronic states with the same parity are allowed. However, selection rules can be different for superconducting artificial atoms. For instance, in the dipole approximation, the interaction Hamiltonian between a flux qubit circuit and a time-dependent magnetic field does not have a well-defined parity, except at the point with a static magnetic flux $f \equiv \Phi/\Phi_0 = \frac{1}{2}$, where Φ is the static magnetic flux applied to the loop and Φ_0 the magnetic-flux quantum. At this particular flux value, the interaction Hamiltonian has odd parity. Owing to the parity symmetries of the artificial-atom states at $f = \frac{1}{2}$, the lowest three levels of the circuit behave like a Ξ -type or ladder-type artificial atom²⁵. In this case, the dipole transition

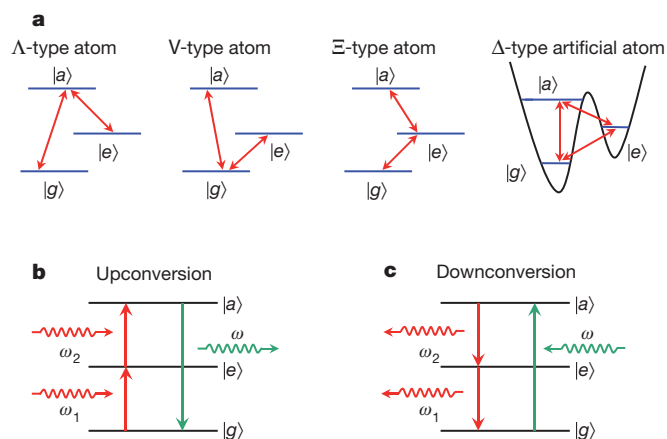


Figure 2 | Three-level atoms and frequency conversions. **a**, Energy levels of natural atoms of the Λ , V and Ξ types, as well as a Δ -type artificial atom consisting of a flux-driven three-junction loop. The allowed dipole transitions between energy levels are indicated in red. In contrast to naturally occurring atoms, the three dipole transitions among the states $|g\rangle$, $|e\rangle$ and $|a\rangle$ are all allowed in the Δ -type three-level artificial atom. Here $|g\rangle$ and $|e\rangle$ denote the ground and first excited states, while $|a\rangle$ denotes either the second or another excited state. **b**, Frequency up-conversion in a Δ -type artificial atom. Here $\omega_1 = (E_e - E_g)/\hbar$, $\omega_2 = (E_a - E_e)/\hbar$ and $\omega = (E_a - E_g)/\hbar$, with E_i ($i = g, e$ or a) being the energy level of the state $|i\rangle$. When two microwave photons, one with frequency ω_1 and the other with ω_2 , are successively absorbed by the artificial atom, it can emit a microwave photon with frequency $\omega = \omega_1 + \omega_2$ via the transition $|a\rangle \rightarrow |g\rangle$. **c**, Frequency down-conversion in the Δ -type artificial atom. When a microwave photon with frequency ω is absorbed by the artificial atom, the sequential transitions $|a\rangle \rightarrow |e\rangle$ and $|e\rangle \rightarrow |g\rangle$ can produce two microwave photons with frequencies ω_1 and ω_2 , respectively. In particular, when $E_a - E_e = E_e - E_g$, the up-conversion in **b** converts two photons with frequency $\frac{1}{2}\omega$ to one photon with frequency ω , while the down-conversion in **c** converts one photon with frequency ω to two photons with frequency $\frac{1}{2}\omega$. Natural atoms cannot perform up- or down-conversion, unless aided by nonlinear effects. However, artificial atoms can.

between $|g\rangle$ and $|a\rangle$ is forbidden, while the other two transitions (among states $|g\rangle$, $|e\rangle$ and $|a\rangle$) are allowed (see Fig. 2a for nomenclature). However, when $f \neq \frac{1}{2}$, the parity symmetry is broken for the interaction Hamiltonian. Therefore, all three dipole transitions among $|g\rangle$, $|e\rangle$ and $|a\rangle$ are possible, allowing the atom to be Δ -type (so called because of the triangle-shaped transitions among the three energy levels, as shown in Fig. 2a). Now (when $f \neq \frac{1}{2}$) the superconducting circuit behaves as a Δ -type cyclic artificial atom, where one- and two-photon processes can coexist²⁵.

This Δ -type artificial atom can be used for up-conversion and down-conversion of the photon frequency (Fig. 2b and c). In these frequency conversions, all transitions involve only linear processes; this is in sharp contrast to conventional frequency conversion in nonlinear optics, where a nonlinear medium is used and the nonlinear effect facilitates converting the frequency of the photons. Recently, the frequency up-conversion of a microwave photon was experimentally demonstrated in a flux qubit²⁶. This experiment explained the observed coexistence of one- and two-photon processes as due to the symmetry-breaking of the system Hamiltonian, when varying the applied magnetic flux away from $f = \frac{1}{2}$.

In the experiment reported in ref. 27, two microwave fields were applied simultaneously to a superconducting circuit containing two coupled flux qubits. The interference between the processes that correspond to a selected excitation by the applied microwave fields can be controlled and used to activate or suppress a given transition. Thus, this method effectively creates artificial and controllable selection rules.

Electromagnetically induced transparency

Quantum interference can be introduced to control the propagation of light through a medium consisting of three-level atoms or qutrits. We now consider a Λ -type three-level atom; to control the propagation of a

probe light field in resonance with the dipole transition $|a\rangle \leftrightarrow |g\rangle$ (that is, at the probe frequency ω_p), one can drive the atom by a second (control) field that is in resonance with the transition $|a\rangle \leftrightarrow |e\rangle$ at the control frequency ω_c ; see Fig. 3. Now the amplitude of the wavefunction for the state $|a\rangle$ is driven by two terms: one proportional to the probability amplitude of the ground state $|g\rangle$ and the other proportional to the probability amplitude of state $|e\rangle$. The combined effect of these two fields is to pump the atom into a coherent superposition of the states $|g\rangle$ and $|e\rangle$ known as a dark state. In such a case, the two driving terms can interfere and cancel each other—that is, they have equal magnitudes but opposite signs. Under this destructive quantum interference, the occupation probability at state $|a\rangle$ is zero, leading to a vanishing light absorption even in the presence of light fields. This effect is called electromagnetically induced transparency (EIT) in quantum optics^{28,29}, and also applies to V- and Ξ -type atoms. This important effect has a variety of applications—for instance, a medium with EIT can slow down and even stop or trap light.

We now consider EIT in a more quantitative manner. Let Ω_p (Ω_c) be the Rabi frequency that quantifies the coupling strength between the probe (control) light and the atom. Here we assume that a Λ -type atom can be prepared in the initial state $|\Psi(0)\rangle = (\Omega_c|g\rangle - \Omega_p|e\rangle)/\Omega$, where $\Omega = \sqrt{\Omega_p^2 + \Omega_c^2}$. When EIT occurs, the atom will be trapped in this dark state, $|\Psi(t)\rangle = (\Omega_c|g\rangle - \Omega_p|e\rangle)/\Omega$, for a time which is dependent on the decoherence rate of the atom. Usually, it is not easy for an atom to be prepared in the initial state $|\Psi(0)\rangle$, when Ω_p is comparable to Ω_c . Instead, the atom can be naturally prepared in the ground state $|g\rangle$. If strong control and weak probe fields are chosen so that $\Omega_c \gg \Omega_p$, the dark state $|\Psi(t)\rangle$ is close to the initial state $|g\rangle$. In such a case, the combined action of the control and probe fields can easily drive the atom from the ground state into the dark state²⁹. This is the reason why a strong control field and a weak probe field are used to experimentally implement EIT in an atomic medium.

At $f = \frac{1}{2}$, the flux qubit circuit can behave like a Ξ -type artificial atom^{25,30}. The circuit can also behave approximately like a Λ -type artificial atom when $f \neq \frac{1}{2}$, if the dipole transition rate between $|g\rangle$ and $|e\rangle$ is much smaller than the rates for the other two transitions³⁰. As discussed above, these selection rules are related to the parity symmetries of the artificial-atom states. In contrast to natural atoms, the tunability of a superconducting circuit can be used to prepare the artificial atom in an initial state that is close to the dark state $|\Psi\rangle$ with

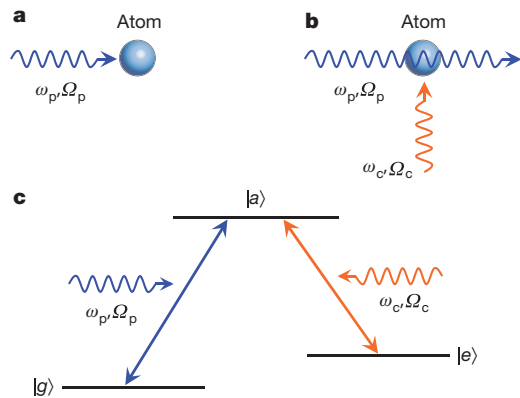


Figure 3 | Electromagnetically induced transparency. **a**, A probe light field is absorbed by natural or artificial atoms when the frequency of the light field is resonant with a particular separation between two atomic energy levels. **b**, However, the probe light field can go through the natural or artificial atoms when a suitable control light field also drives the atoms. **c**, Λ -type three-level atomic system for EIT. The frequency ω_p of the probe light field is resonant with the energy separation between states $|a\rangle$ and $|g\rangle$, and the frequency ω_c of the control light field is resonant with the energy separation between states $|a\rangle$ and $|e\rangle$. The Rabi frequency Ω_p (Ω_c) quantifies the coupling strength between the probe (control) light field and the atom.

arbitrary Ω_c and Ω_p . Therefore, it is experimentally feasible to produce EIT in a single artificial atom for either strong or weak control and probe fields. This is an important advantage of superconducting circuits compared to natural atoms. EIT using superconducting circuits has been studied theoretically (see, for example, refs 31–33) and experimentally^{34,35}. In ref. 35, this phenomenon was experimentally shown using a four-junction loop biased at $f = \frac{1}{2}$, where the circuit behaved as a Ξ -type artificial atom.

State population inversion and lasing

A laser is composed of an amplifying medium inside a resonant optical cavity. When the system is driven, a state population inversion (SPI) can be achieved for the atoms or molecules in the amplifying medium. Moreover, there is positive feedback between the emitted light and the amplifying medium. Because of this positive feedback and the nature of the stimulated photon emission, the laser has a large net optical gain, and the emitted photons have the same direction, phase and polarization. These advantages mean that the laser has a variety of applications in different fields. Recently, several studies have considered lasing using only a single artificial atom, both theoretically^{30,36–38} and experimentally^{39,40}.

With suitable junction parameters, the flux qubit circuit can have the following dipole transition rates³⁰ when $f \neq \frac{1}{2}$: $\Gamma_{ga} > \Gamma_{ae} \gg \Gamma_{eg}$, where the rate Γ_{ij} is proportional to $|t_{ij}|^2$, with t_{ij} being the dipole transition matrix element between states $|i\rangle$ and $|j\rangle$. Because the transition $|a\rangle \rightarrow |e\rangle$ can be dominant over $|e\rangle \rightarrow |g\rangle$, an SPI between states $|e\rangle$ and $|g\rangle$ (Fig. 4a) can be quickly achieved by pumping the artificial atom (via the transition $|g\rangle \rightarrow |a\rangle$) using a strong microwave field. This can be done experimentally by placing the artificial atom in, for example, a coplanar waveguide resonator¹⁶ and sharing a segment of the circuit loop with the transmission line. In the process of achieving an SPI, the weak-coupling regime is assured by having the flux qubit circuit off-resonant with respect to the cavity.

While the SPI is being established, the biasing flux can be adjusted to give a value of f near $\frac{1}{2}$, where the rate Γ_{eg} for the transition $|e\rangle \rightarrow |g\rangle$

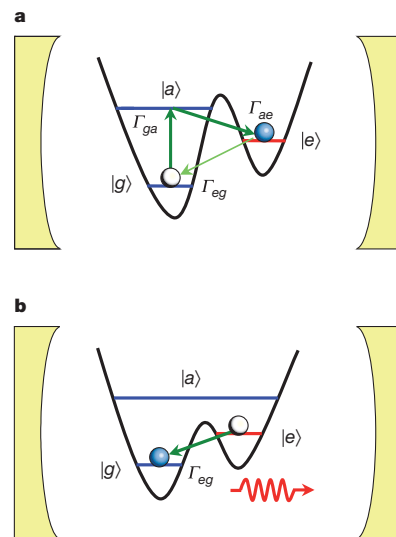


Figure 4 | Lasing. **a**, State population inversion (for lasing) between states $|e\rangle$ and $|g\rangle$ in a three-junction loop at $f > \frac{1}{2}$, where the artificial atom is quickly pumped from $|g\rangle$ to $|a\rangle$ by a strong microwave pulse (for example, by a quick Rabi oscillation) and then decays from $|a\rangle$ to $|e\rangle$ via photon emission. Here the dipole transition rate from $|e\rangle$ to $|g\rangle$ is small because of a higher inter-well barrier between them; the dipole transition rate from $|a\rangle$ to $|e\rangle$ is larger owing to a lower barrier; and the rate is even larger for the dipole transition $|g\rangle \rightarrow |a\rangle$ because no potential barrier is involved in the single well. **b**, Photon emission of the artificial atom to build up a lasing field, where the inter-well barrier is lowered so as to have a strong transition rate between $|e\rangle$ and $|g\rangle$ and to tune the transition $|e\rangle \rightarrow |g\rangle$ into resonance with the cavity.

becomes large and the cavity is resonant with this transition. However, the adiabatic condition is not easy to satisfy near this anticrossing point ($f = \frac{1}{2}$), where the Landau-Zener transition is strong, so the biasing flux cannot be changed very fast while approaching this point. Fortunately, away from this anticrossing point, the Landau-Zener transition is weak, so it is easy to satisfy the adiabatic condition³⁰ and the flux can be changed very quickly. To take advantage of this property, the small Josephson junction in the flux-driven loop can be replaced by a tunable superconducting quantum interference device (SQUID). In this d.c. SQUID, the magnetic field applied to the loop causes the critical current to oscillate with period $2\Phi_0$. With the SPI established at a biasing flux away from $f = \frac{1}{2}$, one can quickly change the flux in the SQUID loop to lower the inter-well barrier, so as to both increase the transition rate Γ_{eg} and tune this transition $|e\rangle \rightarrow |g\rangle$ into resonance with the cavity mode (Fig. 4b). This can yield a strong coupling between the circuit and the cavity.

To build up a lasing field, in addition to the above two conditions for quickly establishing SPI and then achieving a strong circuit-cavity coupling, the cavity used should have a high quality factor Q (Q -factor), that is, a small energy leak or decay rate. This can be implemented using a coplanar waveguide resonator¹⁶.

Indeed, lasing has been experimentally observed using a Cooper-pair box in an on-chip cavity³⁹. In contrast to the proposal³⁰ using a flux-driven loop, this experiment³⁹ employs a different three-level system: the two lowest superconducting states $|g\rangle$ and $|e\rangle$ and a quasi-particle state $|a\rangle$. The gate voltage is tuned to $V_g > e/C_g$ (above the degeneracy point), so state $|2\rangle$ with an extra Cooper pair in the box becomes the ground state $|g\rangle$ of the artificial atom, and state $|0\rangle$ with zero extra Cooper pairs in the box is the excited state $|e\rangle$. Also, the box is connected to a lead via a tunnel barrier. When driving the box with a voltage across the tunnel barrier, an SPI between $|e\rangle \equiv |0\rangle$ and $|g\rangle \equiv |2\rangle$ is achieved, following quasi-particle tunnelling processes³⁶. In ref. 39, lasing was achieved continuously, with emitted light escaping from one end of the cavity.

Cooling

There are different methods for cooling atoms, including Doppler cooling, Sisyphus cooling, side-band cooling, subrecoil cooling, and evaporative cooling⁴¹. Some of these techniques can be adapted to cool a solid-state artificial atom. For instance, the Sisyphus cooling technique has been used to cool a flux qubit (that is, a flux-driven three-junction or four-junction loop)⁴⁰.

Another important advance⁴² is the cooling of a flux qubit implemented via the inverse process of SPI. In ref. 42, the temperature of the superconducting qubit was lowered by up to two orders of magnitude when its surroundings reached a temperature as low as tens of millikelvin. This cooling of the flux qubit is achieved when the biasing flux is shifted away from $f = \frac{1}{2}$, where the dipole transition rates for the lowest three levels of the flux qubit satisfy the relations $\Gamma_{ag} > \Gamma_{ea} \gg \Gamma_{ge}$. By optically pumping the qubit via the transition $|e\rangle \rightarrow |a\rangle$, the qubit is excited to the high-energy state $|a\rangle$ and then decays to the ground state by way of the transition $|a\rangle \rightarrow |g\rangle$ (Fig. 5a), with a net energy, extracted from the qubit, emitted to the outside environment. This experiment also provides fine analogies between solid-state artificial atoms and natural atoms, as well as showing how these analogies can inspire new applications.

Although the superconducting qubit in ref. 42 was greatly cooled ($k_B T \ll E_e - E_g$) in experiments, the noise sources surrounding the qubit were not. So the qubit will quickly return to the temperature of its environment. To overcome this difficulty, the superconducting qubit can be redesigned to increase its controllability by replacing the small Josephson junction in the flux-driven loop with a tunable SQUID⁴³. The cooling process can now be described as follows (Fig 5b–d): first, as in the experiment⁴², the qubit is initially cooled, following the inverse process of SPI. Then, the tunable qubit is switched on for a period of time in order to resonantly interact with the noise source (for example, local two-level fluctuators) surrounding the qubit. This process extracts

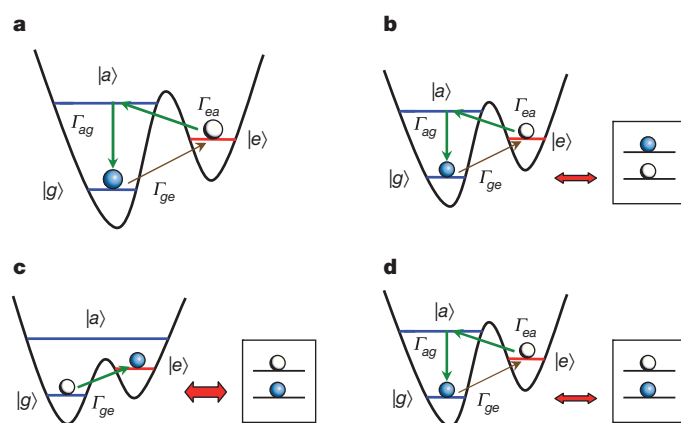


Figure 5 | Cooling a three-level artificial atom and a nearby two-level system. **a**, Cooling the three-junction loop to its ground state $|g\rangle$. While the artificial atom is thermally excited to $|e\rangle$, one can drive the atom to $|a\rangle$ by a microwave field. Because of a large transition rate for $|a\rangle \rightarrow |g\rangle$, the atom can decay quickly from the unstable state $|a\rangle$ to the ground state, emitting net energy, extracted from the atom, to the outside environment. The blue (white) circle denotes the energy level that is occupied (unoccupied) by the artificial atom. The two thick green arrows represent higher-rate dipole transitions, and the thinner brown arrow represents a lower-rate dipole transition. The blue and red levels in the double potential well correspond to the lowest three energy levels of a three-junction loop biased at $f > \frac{1}{2}$. **b**, While the noise source is thermally excited, the artificial atom is shifted off-resonance to the noise source by tuning the externally applied flux and also driven to the cooled state via the inverse process of the state population inversion in **a**. The box to the right of the energy level diagram represents a two-level fluctuator acting as a noise source. **c**, The inter-well barrier of the artificial atom is lowered by tuning the externally applied flux so as to have both a strong transition rate between $|g\rangle$ and $|e\rangle$ and the transition $|g\rangle \rightarrow |e\rangle$ in resonance with the two-level system, so as to extract energy from the two-level system. **d**, Shifting the artificial atom off-resonance from the two-level system and cooling the atom again, with the net energy extracted from the two-level system emitted to the outside environment.

energy from the noise source to heat the qubit. Repeating these two processes⁴³, both the qubit and its neighbouring noise source can be simultaneously cooled. This will significantly enhance the quantum coherence of the qubit, because the cooled qubit is then thermally activated only very slowly to the first excited state.

Recent technical advances allow the fabrication of a nanomechanical resonator with both a high Q -factor and a sufficiently high frequency, close to the typical frequencies of superconducting circuits⁴⁴. This has stimulated researchers to propose different ways to use superconducting circuits to achieve the ground-state cooling of coupled nanomechanical resonators^{37,43,45–48}. Moreover, the experimental cooling of such a resonator, by coupling it to a superconducting single-electron transistor⁴⁹ or to a microwave-frequency superconducting resonator⁵⁰, has also been reported. When a nanomechanical resonator is cooled to the ground state⁵¹, it provides a good platform for exploring various quantum phenomena and for observing the quantum-to-classical transition in such a macroscopic object. This will give rise to the new subject of quantum acoustics.

Photon generation

Superconducting qubits have the advantage of manipulating quantum states in a controllable manner. If these stationary qubits are spatially separated, one can use single photons generated in an extended cavity as a quantum bus, similar to a flying qubit, to implement quantum communication among them (Fig. 6a). Technologically, this requires the generation of single photons by manipulating a superconducting qubit, and the transfer of information between the superconducting qubits and the photons. Using an on-chip cavity, it becomes feasible to achieve this quantum communication process on a chip.

Recent experiments show that a single-photon source can be achieved using a superconducting qubit coupled to an on-chip cavity^{52–55}. When the qubit is prepared in the excited state $|e\rangle$ by a control pulse, it can

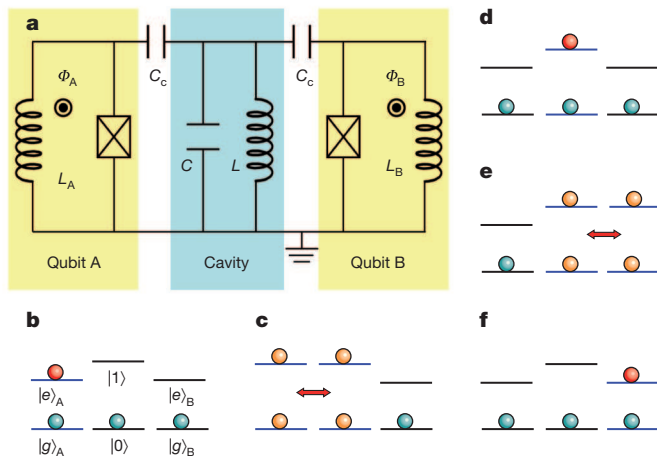


Figure 6 | Transferring quantum information between two stationary qubits via a cavity. **a**, Schematic diagram of two flux-driven phase qubits capacitively coupled by an on-chip cavity (an LC resonator). **b**, Qubit A is prepared in a superposition state $\alpha|g\rangle_A + \beta|e\rangle_A$, while both qubit B and the resonator are prepared in their ground states. In this step, both qubits A and B are off-resonance with the cavity. **c**, Qubit A is shifted into resonance with the resonator, for a time interval $t_1 = \pi/2g_A$, with hg_A being the interaction energy between qubit A and the resonator. This step maps the state of qubit A to the superposition state $\alpha|0\rangle + \beta|1\rangle$ of the resonator, where $|0\rangle$ and $|1\rangle$ are two Fock states of the resonator with zero and one photon, respectively. **d**, Shift qubit A off-resonance with the resonator again, and store the quantum information in the resonator for a time duration t_2 . **e**, Shift qubit B into resonance with the resonator for a time interval $t_3 = \pi/2g_B$, where hg_B is the interaction energy between qubit B and the resonator. This step maps the state of the resonator to the superposition state $\alpha|g\rangle_B + \beta|e\rangle_B$ of qubit B. **f**, Shift qubit B off-resonance with the resonator again, and store the quantum information in qubit B. Note that a high-fidelity state transfer between qubits A and B can be implemented if both the relaxation and decoherence of the state are negligibly small during the above processes.

decay to the ground state $|g\rangle$ by emitting one (and only one) photon in the on-chip cavity; this decay is possible because of the interaction between the qubit and the cavity. If the cavity was originally in the vacuum state $|0\rangle$, it now changes to the single-photon state $|1\rangle$. When the qubit is prepared in an arbitrary superposition state $\alpha|g\rangle + \beta|e\rangle$, in an ideal manner, the coupling between the qubit and the cavity can map the qubit state into a superposition state of zero and one photon in the cavity: $\alpha|0\rangle + \beta|1\rangle$ (Fig. 6b–d). Furthermore, the experiment in ref. 52 shows how to transfer information from a cavity to a stationary qubit (Fig. 6d–f). These experiments demonstrate that both single-photon sources and quantum communication between superconducting qubits can be achieved on a chip. However, because of the relaxation and decoherence in both qubit and cavity, after each step for transferring the information between a stationary qubit and a cavity, the amplitudes α and β of the photon (qubit) state can be different from the amplitudes α and β of the previous qubit (photon) state. Improving relaxation rates and qubit decoherence times should allow higher-fidelity state transfers between qubits and cavities.

In addition to single-photon generation, one can also generate, as proposed in refs 56 and 57, multi-photon Fock states $|n\rangle$ (that is, the number states of photons) and arbitrary superposition states $\sum_n c_n|n\rangle$. Indeed, in a recent experiment⁵⁸, the controlled generation of pure Fock states with up to 15 photons was achieved using a superconducting phase qubit coupled to a microwave on-chip cavity. Moreover, thanks to the advantages of both on-chip cavity and tunable superconducting circuits, complex superpositions of states with different number of photons were also generated in a controlled and deterministic manner⁵⁵, which is a beautiful experimental realization of the protocol described in ref. 56. Recently, the N -photon entangled NOON states, $|N0\rangle + |0N\rangle$, have also been generated in two

superconducting resonators⁵⁹. These experiments further reveal the quantum behaviour of the on-chip cavity and provide a useful on-demand multi-photon source for future quantum-technology applications.

Quantum state tomography

A crucial step in quantum information processing is the measurement of the output quantum states. However, a quantum state cannot be ascertained by a single quantum measurement. This is because quantum states may comprise many complementary features which cannot be measured simultaneously and precisely, owing to uncertainty relations. Nevertheless, all complementary aspects can in principle be observed by a series of measurements on a large enough number of identically prepared copies of the quantum system. Then, one could reconstruct an unknown quantum state from such a complete set of measurements of system observables. Such a process of reconstructing quantum states is called quantum state tomography. Using state tomography, the noisy channel of the quantum system can also be determined. This procedure of determining the dynamics of an open quantum system is known as quantum process tomography.

Tomographic measurements on the quantum states of superconducting charge qubits, either single or multiple qubits, were proposed in ref. 60. Recently, there have been many experiments on the quantum state tomography of single superconducting phase qubits^{61,62} and of two coupled superconducting phase⁶³ and charge⁶⁴ qubits. Also, quantum process tomography was experimentally implemented on single⁶⁵ and two⁶⁶ phase qubits. Indeed, quantum state tomography is an essential tool in qubit-state measurements, and quantum process tomography can be used to probe the noise properties and temporal dynamics of qubit systems.

Future prospects

Given technological advances, superconducting circuits can be used to test quantum mechanics on a macroscopic scale (Box 3). Also, they can be used to demonstrate many novel phenomena in quantum science. A few examples are listed below.

Dynamical Casimir effect

When two parallel mirrors are placed in empty space, their presence affects the vacuum fluctuations of the electromagnetic field. Because of the different densities of the vacuum modes inside and outside the space between the two mirrors, a net force on the mirrors can be generated. This effect of quantum electrodynamics is known as the static Casimir effect.

If the mirrors move, there is also a mismatch between vacuum modes at different times. It has been predicted that this may result in the creation of real photons out of vacuum fluctuations. This dynamical Casimir effect also holds for a single mirror subject to a non-uniform acceleration in empty space. Although receiving considerable interest since its theoretical prediction, there is still no experimental verification of the dynamical Casimir effect. This is mainly due to the fact that the rate of photon production is non-negligible only when the mirror velocity approaches the speed of light, making the use of massive mirrors very challenging. A coplanar waveguide terminated by a SQUID was proposed⁶⁷ for experimentally observing the dynamical Casimir effect. Changing the magnetic flux threading the SQUID loop parametrically modulates the boundary condition of the waveguide and thereby its effective length. Because there is no massive mirror moving, the velocity of the effective boundary can approach the speed of light. Photon production from the vacuum can thus be made experimentally detectable.

Coherent population transfer

Elementary logic gates in quantum computing networks are usually implemented using precisely designed resonant pulses. However, the various fluctuations and operational imperfections that exist in practice limit these designs. Also, the difficulty of switching interbit couplings on

BOX 3

Testing quantum mechanics with macroscopic superconducting circuits

Bell inequality. The Bell inequality shows that the predictions of quantum mechanics can contradict those of local hidden variable theories (see, for example, ref. 92) if one looks at correlations between spatially separated measurements. It can alternatively be stated that no physical theory of local hidden variables can reproduce all of the predictions of quantum mechanics. Tests of the Bell inequality have been proposed, using superconducting circuits such as charge⁹³ and phase qubits⁹⁴. Recently, the violation of the Bell inequality has been experimentally verified⁹⁵ in phase qubits. Because the Bell inequality is violated by a quantum mechanical prediction, this experiment provides strong evidence that these macroscopic superconducting circuits indeed behave quantum mechanically. Recent experimental results^{96,97} on Greenberger–Horne–Zeilinger states do not require statistical arguments for a violation of the Bell inequality to be seen.

Leggett–Garg inequality. Leggett and Garg derived an inequality for a single degree of freedom undergoing coherent oscillations and being measured at successive times⁹⁸. The Leggett–Garg inequality can be regarded as a temporal version of Bell’s inequality, and it should be violated by a quantum two-level system. Very recently, this has been verified experimentally⁹⁹ using a voltage-driven box (that is, the Cooper-pair box) acting as a quantum two-level system, showing that the time correlations present at the detector output violate the inequality.

Kochen–Specker theorem. This theorem elucidates the conflict between quantum mechanics and non-contextual hidden-variable theories⁹². Non-contextuality means that the measured value of an observable is independent of the choice of other co-measurable (commuting) observables that are measured previously or simultaneously. Quantum mechanics is non-contextual, because outcomes depend on the context of measurement. This theorem is an important complement to Bell’s theorem; testing it can disprove non-contextual hidden-variable theories without referring to locality. To confirm such a counterintuitive phenomenon on a macroscopic scale, it was proposed¹⁰⁰ to use two charge qubits, which are controllably coupled by a two-level data-bus built from a phase qubit. The analysis¹⁰⁰ showed that by performing joint non-destructive quantum measurements of two distinct qubits, the proposed superconducting circuits could demonstrate quantum contextuality at a macroscopic level.

and off strongly limits the precise design of the required pulses for two-qubit gates. To overcome these difficulties, ref. 68 proposed an approach to coherently transfer the populations of qubit states by using Stark-chirped rapid adiabatic passages. As in the case of geometric phases, these population transfers are insensitive to the dynamical evolution times of the qubits, as long as they are adiabatic. The rapid adiabatic passages of populations could offer an attractive approach to implementing high-fidelity single- and two-qubit gates for quantum computing.

The key to these rapid adiabatic passages is how to produce time-dependent detunings by chirping the qubit levels. For most natural atomic or molecular systems, where each bound state possesses a definite parity, the required detuning chirps could be achieved by making use of the Stark effect via, for example, two-photon excitations of the qubit levels⁶⁹. The breaking of parity symmetries in the bound states in superconducting circuits such as current-biased Josephson junctions provides an advantage⁶⁸, because the desirable detuning chirps can be produced by single-photon pulses. Recently, rapid adiabatic passage was achieved for the transfer of a single photon in a superconducting circuit⁷⁰.

Tunable mirrors and interferometers

Superconducting circuits can be used for Landau–Zener–Stückelberg interferometry⁷¹, but they can also be used for other types of interferometry—including Fano and Fabry–Perot interferometry^{72,73}—by coupling superconducting qubits to a coplanar waveguide. When injected into the waveguide, the photons interact with the qubits along the way, and can be controlled by changing the applied electric and/or magnetic fields on the qubits. These artificial atoms, working as tunable mirrors, can change the reflection and transmission coefficients of the photons confined in the waveguide.

For a system consisting of a superconducting qubit in an array of coupled cavities, the photon transmission exhibits a more general line shape⁷², beyond the Breit–Wigner and Fano line shapes, because of the nonlinear photonic dispersion relation. At a particular matching condition between the photon wavelength and the lattice constant⁷², the photonic dispersion relation can become linear and the photon transmission has the Breit–Wigner line shape, just as in an open transmission line⁷⁴. Recently, this phenomenon was observed for a superconducting flux qubit coupled to an open transmission line⁷⁵. When two superconducting qubits are placed in an array of coupled cavities, they can be used as tunable mirrors to form a Fabry–Perot interferometer⁷³. Such a controllable on-chip interferometer is expected to have various applications in quantum optics.

Quantum non-demolition measurements

In a quantum measurement, a signal observable of a quantum system is measured by detecting the change in an observable of the detector that is coupled to the quantum system during the process of measurement. Generally, the process of measurement will disturb the state of the quantum system owing to the interplay between the system and the detector. A quantum non-demolition (QND) measurement does not perturb the subsequent evolution of the quantum system; this can be achieved by using a particular type of system–detector coupling that preserves the eigenstates of the signal observable in the quantum system. In quantum optics, a QND measurement of the photon number can be implemented using the optical Kerr effect and a dispersive atom–field coupling (see, for example, ref. 29).

The first successful QND measurement on a superconducting qubit was implemented using the dispersive atom–field coupling technique^{16,76}. Recent experiments^{77,78} show that QND measurements can also be implemented for a single superconducting qubit by using a nonlinear resonator as the detector. In ref. 77, the detector was composed of a SQUID shunted with a capacitance, while in ref. 78 the detector was a bifurcation amplifier, which is a r.f.-driven Josephson junction working near the dynamical bifurcation point⁷⁹. Very recently, a fast QND measurement of a flux qubit was implemented in the weakly projective regime by employing a hysteretic d.c. SQUID detector⁸⁰. A quantum device can have multiple qubits, so QND measurements on quantum states of multiple qubits (for example, entangled states) should be an appealing topic for future investigations.

Generating squeezed states

Squeezed states have been extensively studied in quantum optics, and are now being studied in condensed matter systems. Owing to their tunable nonlinearity and low losses in the microwave regime, Josephson-junction superconducting circuits are promising devices for producing squeezed states. In superconducting circuits, LC oscillators have been successfully used for quantum control and readout devices in conjunction with superconducting qubits. As parametric transducers (essentially, radio-frequency auto-oscillators), superconducting resonant tank circuits have been used to measure the quantum state of flux qubits⁸¹. When squeezed states are generated in these resonant tank circuits acting as quantum-state detectors, the noise of the detectors can be decreased below the standard quantum limit. A recent theoretical study⁸² shows that a superconducting parametric transducer can naturally implement this approach, as it can be used both to produce squeezed states and to use

them in order to minimize quantum fluctuations. An immediate application of this method would be to suppress the effective noise temperature of the amplifier connected to the parametric transducer, at least to the nominal temperature of the cooling chamber.

Topological phases

A topologically protected quantum state degeneracy cannot be lifted by any local perturbations⁸³. It is therefore natural to consider using topological phases for applications requiring a high degree of quantum coherence. With superconducting circuits as building blocks, various artificial lattices can be constructed that possess interesting topological phases. For instance, it has been proposed that a triangular Josephson junction array may have a twofold degenerate ground state, which could be used for constructing topologically protected qubits⁸⁴. Recently, an experiment⁸⁵ was implemented for a prototype device that consisted of 12 physical qubits made of nanoscale Josephson junctions. Owing to properly tuned quantum fluctuations, this system was protected against magnetic flux variations well beyond linear order. This suggests that topologically protected superconducting qubits are feasible. Also, superconducting circuits were proposed⁸⁶ as a way to construct the Kitaev honeycomb model, which requires that the spin (natural or artificial) at each node of a honeycomb lattice interacts with its three nearest neighbours through three different types of interactions⁸⁷. Depending on the bond parameters, this anisotropic spin model supports both Abelian and non-Abelian anyons, which are particles obeying unusual statistics (they are neither bosons nor fermions). Its realization would provide exciting opportunities for experimentally demonstrating anyons.

Final remarks

The superconducting circuits that we have described above contain Josephson junctions that can act as nonlinear inductors. Using suitably designed superconducting circuits, it is therefore possible to fabricate field-controlled nonlinear resonators, which can be used to demonstrate the Kerr effect (either quadratic electro-optic or quadratic magneto-optic). If such circuits were used as a Kerr medium, one could carry out a variety of nonlinear optics experiments—for example, coupling microwave photons, implementing quantum gates for photon qubits, and performing QND measurements. Superconducting circuits could have many other applications. For instance, it has been suggested that a coplanar waveguide with the centre conductor replaced by an array of SQUIDs could be used to simulate Hawking radiation⁸⁸. Indeed, superconducting circuits have the advantage of enabling the study of complex controllable quantum dynamics. This could lead to quantum simulations and on-chip studies of many-body physics. Numerous new phenomena and applications will continue to be discovered using superconducting circuits, and these will play an important part in future quantum technologies.

1. Makhlin, Y., Schön, G. & Shnirman, A. Quantum-state engineering with Josephson-junction devices. *Rev. Mod. Phys.* **73**, 357–400 (2001).
2. You, J. Q. & Nori, F. Superconducting circuits and quantum information. *Phys. Today* **58**, 42–47 (2005).
3. Clarke, J. & Wilhelm, F. K. Superconducting quantum bits. *Nature* **453**, 1031–1042 (2008).
4. Schoelkopf, R. J. & Girvin, S. M. Wiring up quantum systems. *Nature* **451**, 664–669 (2008).
5. Nakamura, Y., Pashkin, Yu A. & Tsai, J. S. Coherent control of macroscopic quantum states in a single-Cooper-pair box. *Nature* **398**, 786–788 (1999).
6. van der Wal, C. H. et al. Quantum superposition of macroscopic persistent-current states. *Science* **290**, 773–777 (2000).
7. Vion, D. et al. Manipulating the quantum state of an electrical circuit. *Science* **296**, 886–889 (2002).
8. Yu, Y., Han, S. Y., Chu, X., Chu, S. I. & Wang, Z. Coherent temporal oscillations of macroscopic quantum states in a Josephson junction. *Science* **296**, 889–892 (2002).
9. Martinis, J. M., Nam, S., Aumentado, J. & Urbina, C. Rabi oscillations in a large Josephson-junction qubit. *Phys. Rev. Lett.* **89**, 117901 (2002).
10. You, J. Q., Hu, X., Ashhab, S. & Nori, F. Low-decoherence flux qubit. *Phys. Rev. B* **75**, 140515 (2007).
11. Steffen, M. et al. High-coherence hybrid superconducting qubit. *Phys. Rev. Lett.* **105**, 100502 (2010).

Report of a low-decoherence flux qubit experiment.

12. Koch, J. et al. Charge-insensitive qubit design derived from the Cooper pair box. *Phys. Rev. A* **76**, 042319 (2007).
13. You, J. Q. & Nori, F. Quantum information processing with superconducting qubits in a microwave field. *Phys. Rev. B* **68**, 064509 (2003).
14. Blais, A., Huang, R.-S., Wallraff, A., Girvin, S. M. & Schoelkopf, R. J. Cavity quantum electrodynamics for superconducting electrical circuits: an architecture for quantum computation. *Phys. Rev. A* **69**, 062320 (2004).
15. Chiorescu, I. et al. Coherent dynamics of a flux qubit coupled to a harmonic oscillator. *Nature* **431**, 159–162 (2004).
16. Wallraff, A. et al. Strong coupling of a single photon to a superconducting qubit using circuit quantum electrodynamics. *Nature* **431**, 162–167 (2004).
17. Fragner, A. et al. Resolving vacuum fluctuations in an electrical circuit by measuring the Lamb shift. *Science* **322**, 1357–1360 (2008).
18. Devoret, M. H., Girvin, S. & Schoelkopf, R. Circuit-QED: how strong can the coupling between a Josephson junction atom and a transmission line resonator be? *Ann. Phys. (Leipz.)* **16**, 767–779 (2007).
19. Zueco, D., Reuther, G. M., Kohler, S. & Hänggi, P. Qubit-oscillator dynamics in the dispersive regime: analytical theory beyond the rotating-wave approximation. *Phys. Rev. A* **80**, 033846 (2009).
20. Ashhab, S. & Nori, F. Qubit-oscillator systems in the ultrastrong-coupling regime and their potential for preparing nonclassical states. *Phys. Rev. A* **81**, 042311 (2010).
21. Nataf, P. & Ciuti, C. Vacuum degeneracy of a circuit QED system in the ultrastrong coupling regime. *Phys. Rev. Lett.* **104**, 023601 (2010).
22. Niemczyk, T. et al. Circuit quantum electrodynamics in the ultrastrong-coupling regime. *Nature Phys.* **6**, 772–776 (2010).
23. Forn-Díaz, P. et al. Observation of the Bloch-Siegert shift in a qubit-oscillator system in the ultrastrong coupling regime. *Phys. Rev. Lett.* **105**, 237001 (2010).
24. Wilson, C. M. et al. Coherence times of dressed states of a superconducting qubit under extreme driving. *Phys. Rev. Lett.* **98**, 257003 (2007).
25. Liu, Y. X., You, J. Q., Wei, L. F., Sun, C. P. & Nori, F. Optical selection rules and phase-dependent adiabatic state control in a superconducting quantum circuit. *Phys. Rev. Lett.* **95**, 087001 (2005).
26. Deppe, F. et al. Two-photon probe of the Jaynes-Cummings model and controlled symmetry breaking in circuit QED. *Nature Phys.* **4**, 686–691 (2008).
27. de Groot, P. C. et al. Selective darkening of degenerate transitions demonstrated with two superconducting quantum bits. *Nature Phys.* **6**, 763–766 (2010).
28. Harris, S. E. Electromagnetically induced transparency. *Phys. Today* **50**, 36–42 (1997).
29. Scully, M. O. & Zubairy, M. S. *Quantum Optics* (Cambridge Univ. Press, 1997).
30. You, J. Q., Liu, Y. X., Sun, C. P. & Nori, F. Persistent single-photon production by tunable on-chip micromaser with a superconducting quantum circuit. *Phys. Rev. B* **75**, 104516 (2007).
31. Murali, K. V. R. M., Dutton, Z., Oliver, W. D., Crankshaw, D. S. & Orlando, T. P. Probing decoherence with electromagnetically induced transparency in superconductive quantum circuits. *Phys. Rev. Lett.* **93**, 087003 (2004).
32. Dutton, Z., Murali, K. V. R. M., Oliver, W. D. & Orlando, T. P. Electromagnetically induced transparency in superconducting quantum circuits: effects of decoherence, tunneling, and multilevel crosstalk. *Phys. Rev. B* **73**, 104516 (2006).
33. Ian, H., Liu, Y. X. & Nori, F. Tunable electromagnetically induced transparency and absorption with dressed superconducting qubits. *Phys. Rev. A* **81**, 063823 (2010).
34. Sillanpää, M. A. et al. Autler-Townes effect in a superconducting three-level system. *Phys. Rev. Lett.* **103**, 193601 (2009).
35. Abdumalikov, A. A. Jr et al. Electromagnetically induced transparency on a single artificial atom. *Phys. Rev. Lett.* **104**, 193601 (2010).
36. Rodrigues, D. A., Imbers, J. & Armour, A. D. Quantum dynamics of a resonator driven by a superconducting single-electron transistor: a solid-state analogue of the micromaser. *Phys. Rev. Lett.* **98**, 067204 (2007).
37. Hauss, J., Fedorov, A., Hutter, C., Shnirman, A. & Schön, G. Single-qubit lasing and cooling at the Rabi frequency. *Phys. Rev. Lett.* **100**, 037003 (2008).
38. Ashhab, S., Johansson, J. R., Zagoskin, A. M. & Nori, F. Single-artificial-atom lasing using a voltage-biased superconducting charge qubit. *N. J. Phys.* **11**, 023030 (2009).
39. Astafiev, O. et al. Single artificial-atom lasing. *Nature* **449**, 588–590 (2007).
40. Grajcar, M. et al. Sisyphus cooling and amplification by a superconducting qubit. *Nature Phys.* **4**, 612–616 (2008).
41. Meystre, P. *Atom Optics* (Springer, 2001).
42. Valenzuela, S. O. et al. Microwave-induced cooling of a superconducting qubit. *Science* **314**, 1589–1592 (2006).
43. You, J. Q., Liu, Y. X. & Nori, N. Simultaneous cooling of an artificial atom and its neighboring quantum system. *Phys. Rev. Lett.* **100**, 047001 (2008).
44. Huang, X. M. H., Zorman, C. A., Mehregany, M. & Roukes, M. L. Nanodevice motion at microwave frequencies. *Nature* **421**, 496 (2003).
45. Martin, I., Shnirman, A., Tian, L. & Zoller, P. Ground-state cooling of mechanical resonators. *Phys. Rev. B* **69**, 125339 (2004).

46. Zhang, P., Wang, Y. D. & Sun, C. P. Cooling mechanism for a nonmechanical resonator by periodic coupling to a Cooper pair box. *Phys. Rev. Lett.* **95**, 097204 (2005).
47. Marquardt, F., Chen, J. P., Clerk, A. A. & Girvin, S. M. Quantum theory of cavity-assisted sideband cooling of mechanical motion. *Phys. Rev. Lett.* **99**, 093902 (2007).
48. Grajcar, M., Ashhab, S., Johansson, J. R. & Nori, F. Lower limit on the achievable temperature in resonator-based sideband cooling. *Phys. Rev. B* **78**, 035406 (2008).
49. Naik, A. *et al.* Cooling a nanomechanical resonator with quantum back-action. *Nature* **443**, 193–196 (2006).
50. Rocheleau, T. *et al.* Preparation and detection of a mechanical resonator near the ground state of motion. *Nature* **463**, 72–75 (2010); published online 9 December 2009.
51. O'Connell, A. D. *et al.* Quantum ground state and single-phonon control of a mechanical resonator. *Nature* **464**, 697–703 (2010).
52. Sillanpää, M. A., Park, J. I. & Simmonds, R. W. Coherent quantum state storage and transfer between two phase qubits via a resonant cavity. *Nature* **449**, 438–442 (2007).
- Report of quantum-information transfer between two superconducting qubits using single photons generated in a cavity as a quantum bus.**
53. Houck, A. A. *et al.* Generating single microwave photons in a circuit. *Nature* **449**, 328–331 (2007).
54. Hofheinz, M. *et al.* Generation of Fock states in a superconducting quantum circuit. *Nature* **454**, 310–314 (2008).
55. Hofheinz, M. *et al.* Synthesizing arbitrary quantum states in a superconducting resonator. *Nature* **459**, 546–549 (2009).
- Report of the controllable and deterministic generation of complex superpositions of states with different number of photons by using superconducting circuits.**
56. Law, C. K. & Eberly, J. H. Arbitrary control of a quantum electromagnetic field. *Phys. Rev. Lett.* **76**, 1055–1058 (1996).
57. Liu, Y. X., Wei, L. F. & Nori, F. Generation of nonclassical photon states using a superconducting qubit in a microcavity. *Europhys. Lett.* **67**, 941–947 (2004).
58. Wang, H. *et al.* Measurement of the decay of Fock states in a superconducting quantum circuit. *Phys. Rev. Lett.* **101**, 240401 (2008).
59. Wang, H. *et al.* Deterministic entanglement of photons in two superconducting microwave resonators. *Phys. Rev. Lett.* **106**, 060401 (2011).
60. Liu, Y. X., Wei, L. F. & Nori, F. Tomographic measurements on superconducting qubit states. *Phys. Rev. B* **72**, 014547 (2005).
61. Steffen, M. *et al.* State tomography of capacitively shunted phase qubits with high fidelity. *Phys. Rev. Lett.* **97**, 050502 (2006).
62. Katz, N. *et al.* Coherent state evolution in a superconducting qubit from partial-collapse measurement. *Science* **312**, 1498–1500 (2006).
63. Steffen, M. *et al.* Measurement of the entanglement of two superconducting qubits via state tomography. *Science* **313**, 1423–1425 (2006).
64. Filipp, S. *et al.* Two-qubit state tomography using a joint dispersive readout. *Phys. Rev. Lett.* **102**, 200402 (2009).
65. Neeley, M. *et al.* Process tomography of quantum memory in a Josephson-phase qubit coupled to a two-level state. *Nature Phys.* **4**, 523–526 (2008).
66. Bialczak, R. C. *et al.* Quantum process tomography of a universal entangling gate implemented with Josephson phase qubits. *Nature Phys.* **6**, 409–413 (2010).
67. Johansson, J. R., Johansson, G., Wilson, C. M. & Nori, F. Dynamical Casimir effect in a superconducting coplanar waveguide. *Phys. Rev. Lett.* **103**, 147003 (2009).
68. Wei, L. F., Johansson, J. R., Cen, L. X., Ashhab, S. & Nori, F. Controllable coherent population transfers in superconducting qubits for quantum computing. *Phys. Rev. Lett.* **100**, 113601 (2008).
69. Rangelov, A. A. *et al.* Stark-shift-chirped rapid-adiabatic-passage technique among three states. *Phys. Rev. A* **72**, 053403 (2005).
70. Johnson, B. R. *et al.* Quantum non-demolition detection of single microwave photons in a circuit. *Nature Phys.* **6**, 663–667 (2010).
71. Shevchenko, S. N., Ashhab, S. & Nori, F. Landau-Zener-Strückelberg interferometry. *Phys. Rep.* **492**, 1–30 (2010).
72. Zhou, L., Gong, Z. R., Liu, Y. X., Sun, C. P. & Nori, F. Controllable scattering of a single photon inside a one-dimensional resonator waveguide. *Phys. Rev. Lett.* **101**, 100501 (2008).
73. Zhou, L., Dong, H., Liu, Y. X., Sun, C. P. & Nori, F. Quantum supercavity with atomic mirrors. *Phys. Rev. A* **78**, 063827 (2008).
74. Shen, J. T. & Fan, S. Coherent single photon transport in a one-dimensional waveguide coupled with superconducting quantum bits. *Phys. Rev. Lett.* **95**, 213001 (2005).
75. Astafiev, O. *et al.* Resonance fluorescence of a single artificial atom. *Science* **327**, 840–843 (2010).
76. Wallraff, A. *et al.* Approaching unit visibility for control of a superconducting qubit with dispersive readout. *Phys. Rev. Lett.* **95**, 060501 (2005).
77. Lupaşcu, A. *et al.* Quantum non-demolition measurement of a superconducting two-level system. *Nature Phys.* **3**, 119–125 (2007).
78. Boulant, N. *et al.* Quantum nondemolition readout using a Josephson bifurcation amplifier. *Phys. Rev. B* **76**, 014525 (2007).
79. Siddiqi, I. *et al.* RF-driven Josephson bifurcation amplifier for quantum measurement. *Phys. Rev. Lett.* **93**, 207002 (2004).
80. Picot, T., Schouten, R., Harmans, C. J. P. M. & Mooij, J. E. Quantum nondemolition measurement of a superconducting qubit in the weakly projective regime. *Phys. Rev. Lett.* **105**, 040506 (2010).
81. Il'ichev, E. *et al.* Continuous monitoring of Rabi oscillations in a Josephson flux qubit. *Phys. Rev. Lett.* **91**, 097906 (2003).
82. Zagoskin, A. M., Il'ichev, E., McCutcheon, M. W., Young, J. F. & Nori, F. Controlled generation of squeezed states of microwave radiation in a superconducting resonant circuit. *Phys. Rev. Lett.* **101**, 253602 (2008).
83. Nayak, C., Simon, S. H., Stern, A., Freedman, M. & Das Sarma, S. Non-Abelian anyons and topological quantum computation. *Rev. Mod. Phys.* **80**, 1083–1159 (2008).
84. Ioffe, L. B. *et al.* Topologically protected quantum bits using Josephson junction arrays. *Nature* **415**, 503–506 (2002).
85. Gladchenko, S. *et al.* Superconducting nanocircuits for topologically protected qubits. *Nature Phys.* **5**, 48–53 (2009); published online 30 November 2008.
86. You, J. Q., Shi, X. F., Hu, X. & Nori, F. Quantum emulation of a spin system with topologically protected ground states using superconducting quantum circuits. *Phys. Rev. B* **81**, 014505 (2010).
87. Kitaev, A. Anyons in an exactly solved model and beyond. *Ann. Phys.* **321**, 2–111 (2006).
88. Nation, P. D., Blencowe, M. P., Rimberg, A. J. & Buks, E. Analogue Hawking radiation in a dc-SQUID array transmission line. *Phys. Rev. Lett.* **103**, 087004 (2009).
89. Friedman, J. R., Patel, V., Chen, W., Tolpygo, S. K. & Lukens, J. E. Quantum superposition of distinct macroscopic states. *Nature* **406**, 43–46 (2000).
90. Bertet, P. *et al.* Dephasing of a superconducting qubit induced by photon noise. *Phys. Rev. Lett.* **95**, 257002 (2005).
91. Simmonds, R. W. *et al.* Decoherence in Josephson phase qubits from junction resonators. *Phys. Rev. Lett.* **93**, 077003 (2004).
92. Genovesi, M. Research on hidden variable theories: a review of recent progresses. *Phys. Rep.* **413**, 319–396 (2005).
93. Wei, L. F., Liu, Y. X. & Nori, F. Testing Bell's inequality in a constantly coupled Josephson circuit by effective single-qubit operations. *Phys. Rev. B* **72**, 104516 (2005).
94. Kofman, A. G. & Korotkov, A. N. Analysis of Bell inequality violation in superconducting phase qubits. *Phys. Rev. A* **77**, 104502 (2008).
95. Ansmann, M. *et al.* Violation of Bell's inequality in Josephson phase qubits. *Nature* **461**, 504–506 (2009).
96. Neeley, M. *et al.* Generation of three-qubit entangled states using superconducting phase qubits. *Nature* **467**, 570–573 (2010).
97. DiCarlo, L. *et al.* Preparation and measurement of three-qubit entanglement in a superconducting circuit. *Nature* **467**, 574–578 (2010).
98. Leggett, A. J. & Garg, A. Quantum mechanics versus macroscopic realism: is the flux there when nobody looks? *Phys. Rev. Lett.* **54**, 857–860 (1985).
99. Palacios-Laloy, A. *et al.* Experimental violation of a Bell's inequality in time with weak measurement. *Nature Phys.* **6**, 442–447 (2010).
100. Wei, L. F., Maruyama, K., Wang, X. B., You, J. Q. & Nori, F. Testing quantum contextuality with macroscopic superconducting circuits. *Phys. Rev. B* **81**, 174513 (2010).

Acknowledgements We thank S. Ashhab for comments on the manuscript. J.Q.Y. acknowledges partial support from the National Basic Research Program of China (grant no. 2009CB929300), the National Natural Science Foundation of China (grant no. 10625416), the ISTCP (grant no. 2008DFA01930) and the MOE of China (grant no. B06011). F.N. acknowledges partial support from the Laboratory of Physical Sciences, National Security Agency, Army Research Office, DARPA, AFOSR, the National Science Foundation (grant no. 0726909), JSPS-RFBR (contract no. 09-02-92114), a Grant-in-Aid for Scientific Research (S), MEXT Kakenhi on Quantum Cybernetics, and the JSPS through its FIRST programme.

Author Contributions Both authors developed the framework for the Review, participated in literature review and discussions, and contributed to the writing.

Author Information Reprints and permissions information is available at www.nature.com/reprints. The authors declare no competing financial interests. Readers are welcome to comment on the online version of this article at www.nature.com/nature. Correspondence should be addressed to F.N. (fnori@riken.jp) and J.Q.Y. (jqyou@fudan.edu.cn).