

Oversampling Example

Given: 2nd order analog filter $H_z(j\Omega) = \frac{(200\pi)^2}{(j\Omega + 200\pi)^2}$

Signal BW $-50 < f < 50$ Hz

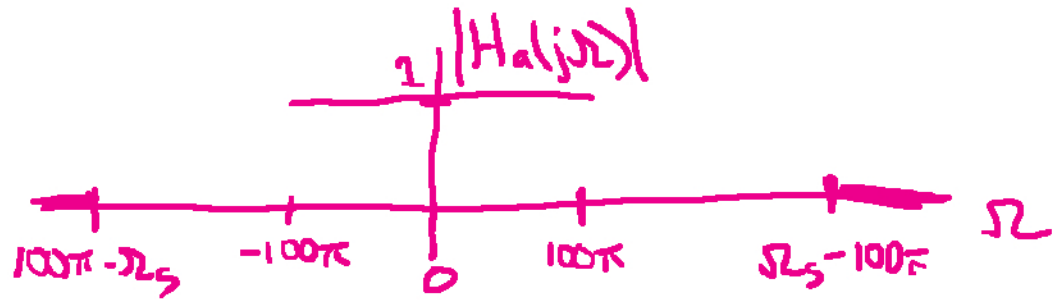
Evaluate $|H_z(j\Omega)|$ for: anti-aliasing filter,
zero-order hold anti-imaging filter

1) Sampling frequency = 300 Hz

2) Sampling frequency = 2400 Hz (8x oversampling)

Ideal anti-aliasing filter

2

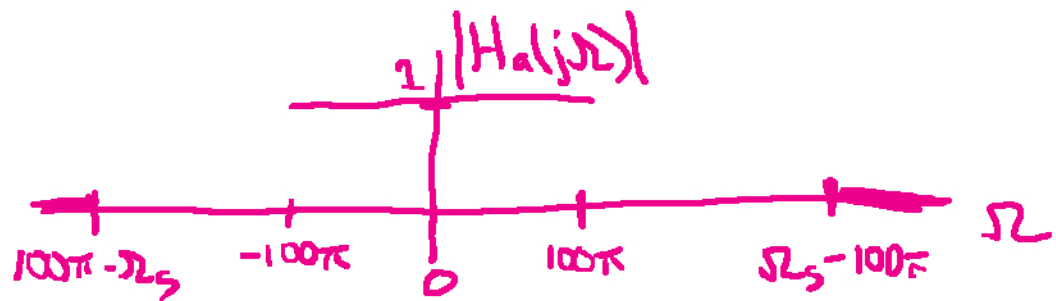


$$|H_a(j\Omega)| = \begin{cases} 1 & , |\Omega| < 100\pi \\ 0 & , |\Omega| > \Omega_s - 100\pi \end{cases}$$

$$1) \Omega_s = 600\pi ; 2) \Omega_s = 4800\pi$$

Ideal anti-aliasing filter

2



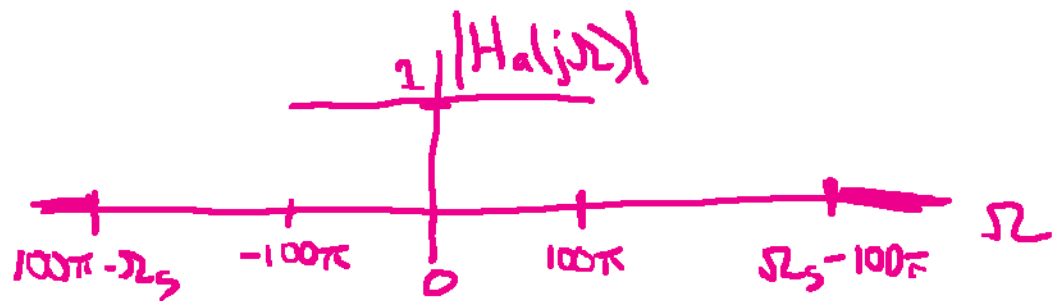
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Passband constraint same for 1) + 2)

$$|H_2(j100\pi)| = \frac{(200\pi)^2}{|240\pi(j^{1/2} + 1)|^2} = 4/5 = 0.8$$

Ideal anti-aliasing filter



$$|H_a(j\Omega)| = \begin{cases} 1 & , |\Omega| < 100\pi \\ 0 & , |\Omega| > \Omega_s - 100\pi \end{cases}$$

1) $\Omega_s = 600\pi$; 2) $\Omega_s = 4800\pi$

Passband constraint same for 1) + 2)

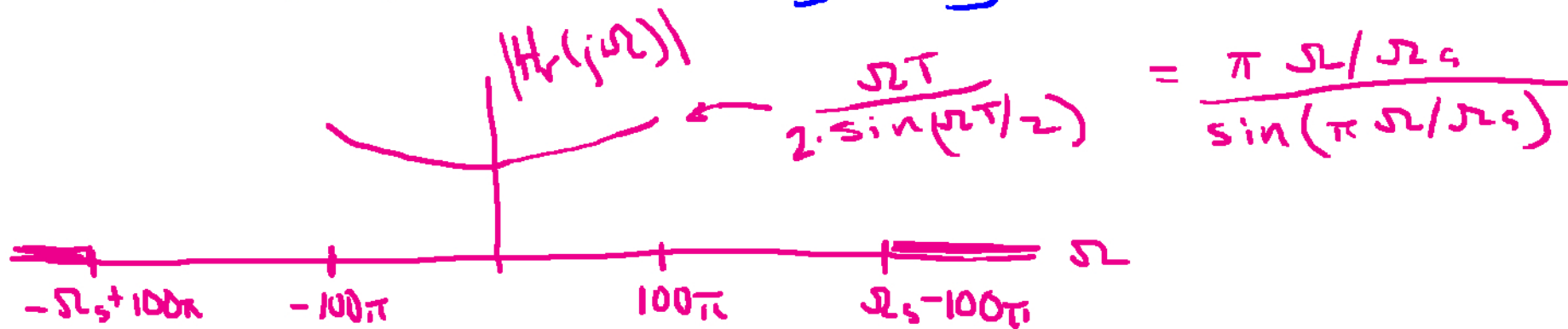
$$|H_2(j100\pi)| = \frac{(200\pi)^2}{|200\pi(j^{1/2} + 1)|^2} = 4/5 = 0.8$$

Stopband actual

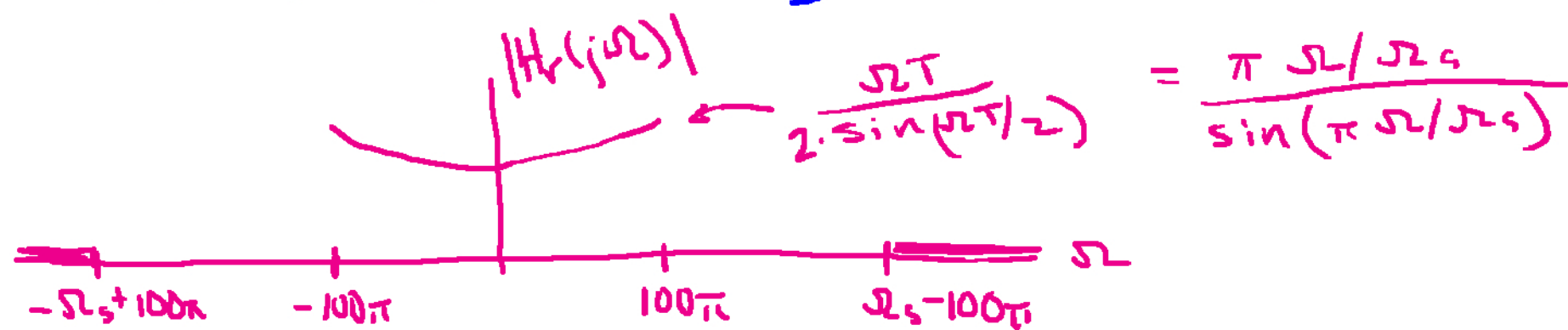
$$1) |H_2(j500\pi)| = \frac{(200\pi)^2}{|200\pi(j^{5/2} + 1)|^2} = \frac{4}{29} \approx 0.14$$

$$2) |H_2(j4700\pi)| = \frac{(200\pi)^2}{|200\pi(j^{47/2} + 1)|^2} = \frac{4}{47^2 + 4} \approx 0.002 \quad (\text{76 x atten. of 1})$$

Ideal Anti-imaging Filter



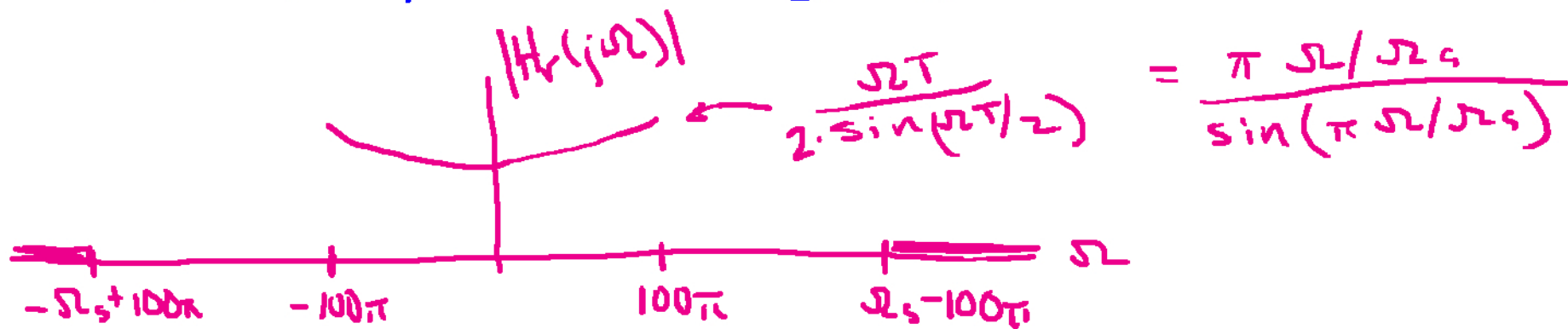
Ideal Anti-imaging Filter



1) $\Omega_s = 600\pi$; Desired gain at $\Omega = 100\pi$ $|H_r(j100\pi)| = \frac{\pi/6}{\sin(\pi/6)} \approx 1.05$

Actual filter: $\Omega = 100\pi$, $|H_2(j100\pi)| = 0.8$
 Stopband $\Omega = 500\pi$, $|H_2(j500\pi)| \approx 0.14$

Ideal Anti-imaging Filter



1) $\Omega_s = 600\pi$; Desired gain at $\Omega = 100\pi$ $|H_r(j100\pi)| = \frac{\pi/6}{\sin(\pi/6)} \approx 1.05$

Actual filter: $\Omega = 100\pi$, $|H_2(j100\pi)| = 0.8$

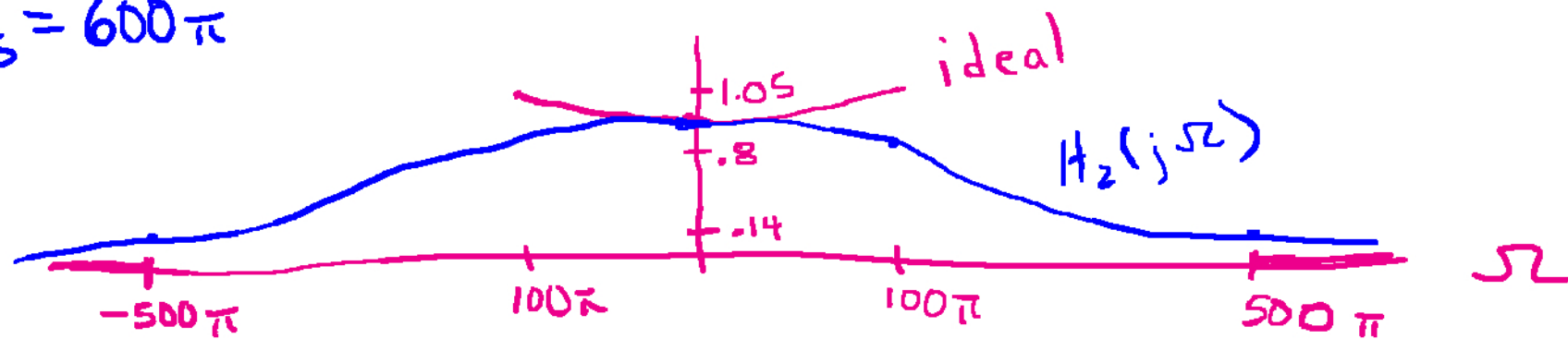
stopband $\Omega = 500\pi$, $|H_2(j500\pi)| \approx 0.14$

2) $\Omega_s = 4800\pi$; Desired gain at $\Omega = 100\pi$ $|H_r(j100\pi)| = \frac{\pi/48}{\sin(\pi/48)} \approx 1.007$

Actual filter: $\Omega = 100\pi$, $|H_2(j100\pi)| = 0.8$

stopband $\Omega = 4700\pi$ $|H_2(j4700\pi)| \approx 0.002$ (≈ 76 more
often
than 1)

1) $\Omega_s = 600\pi$



2) $\Omega_s = 4800\pi$

