

# Signal Notation and Properties

# Contents

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## I. Signals as functions

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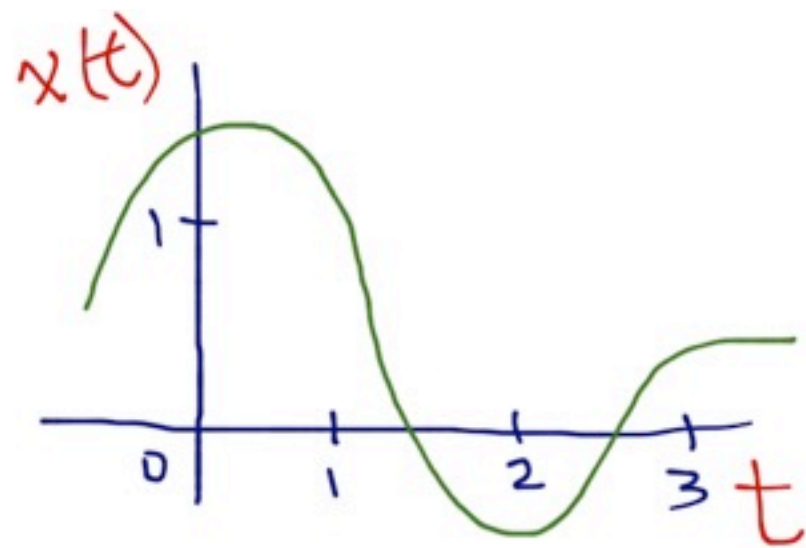
1. Signals as functions
2. Continuous- and discrete-time signals

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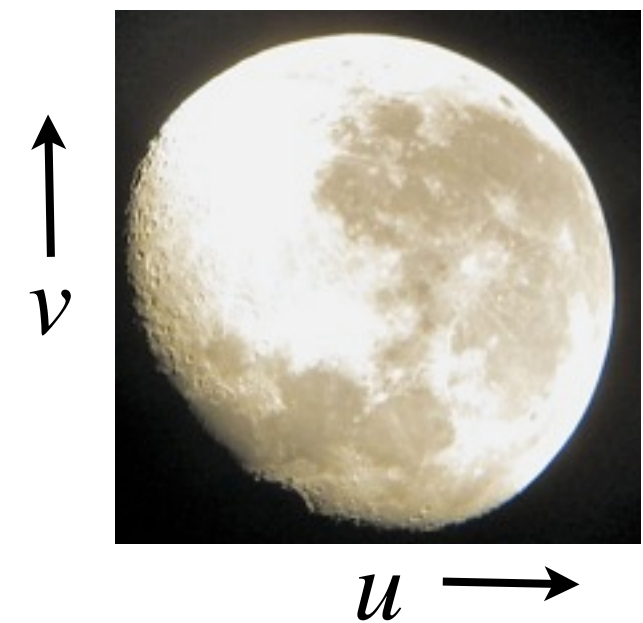
1. Signals as functions
2. Continuous- and discrete-time signals
3. Periodic signals

# Signals

$x(t)$

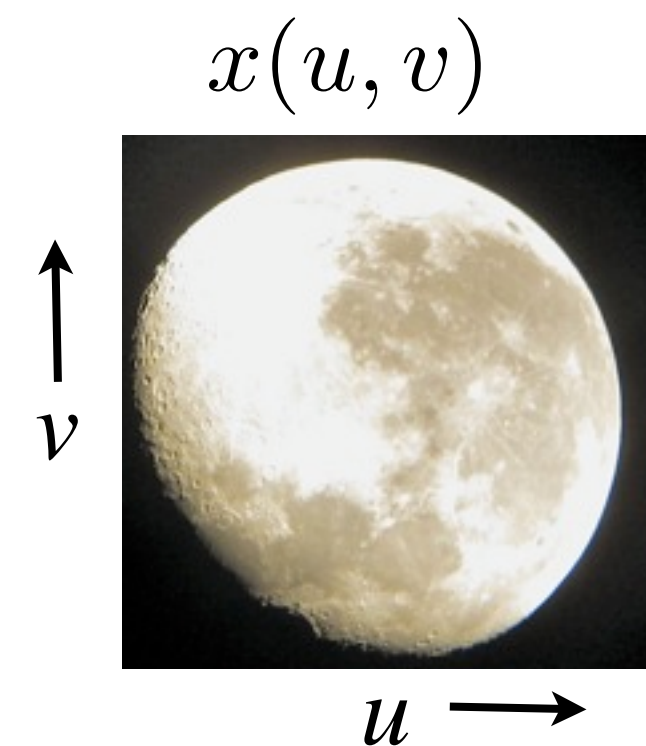
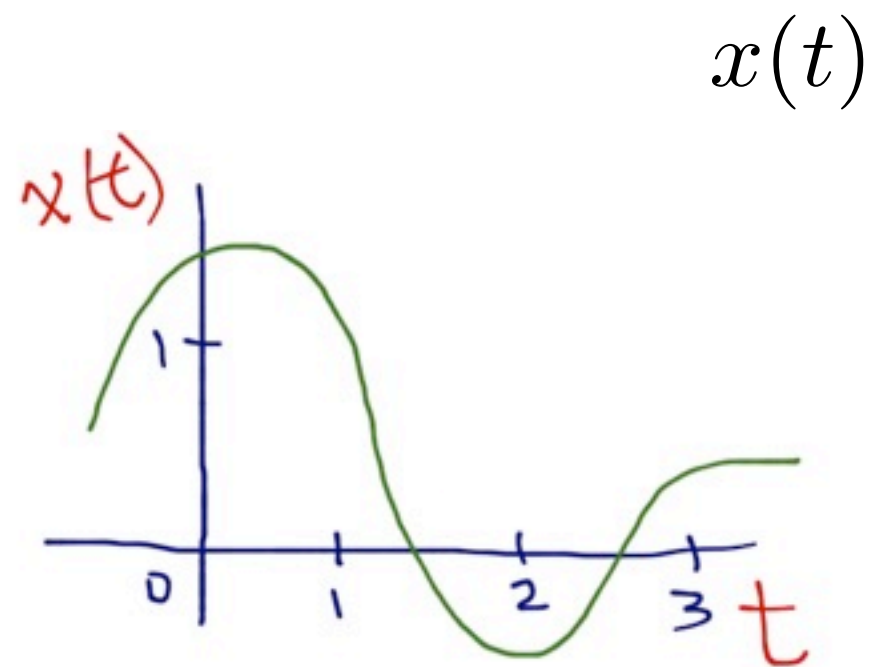


$x(u, v)$



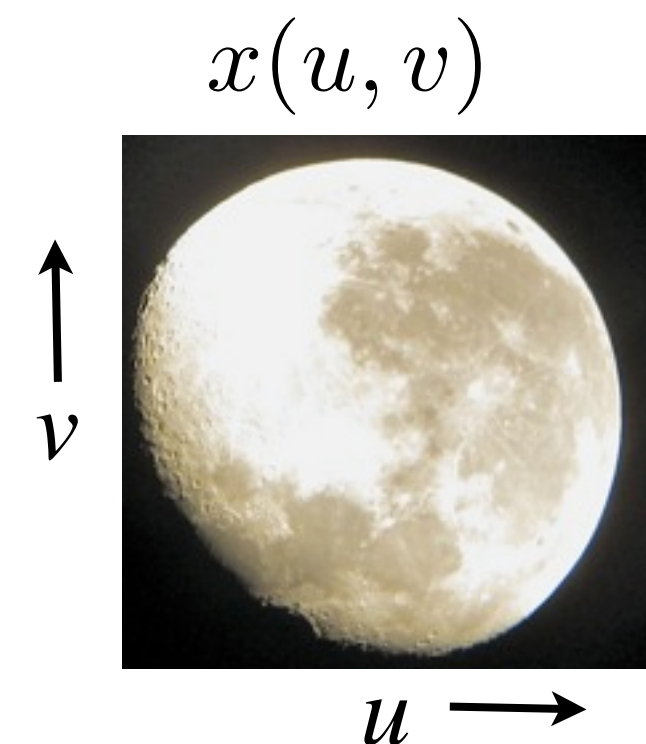
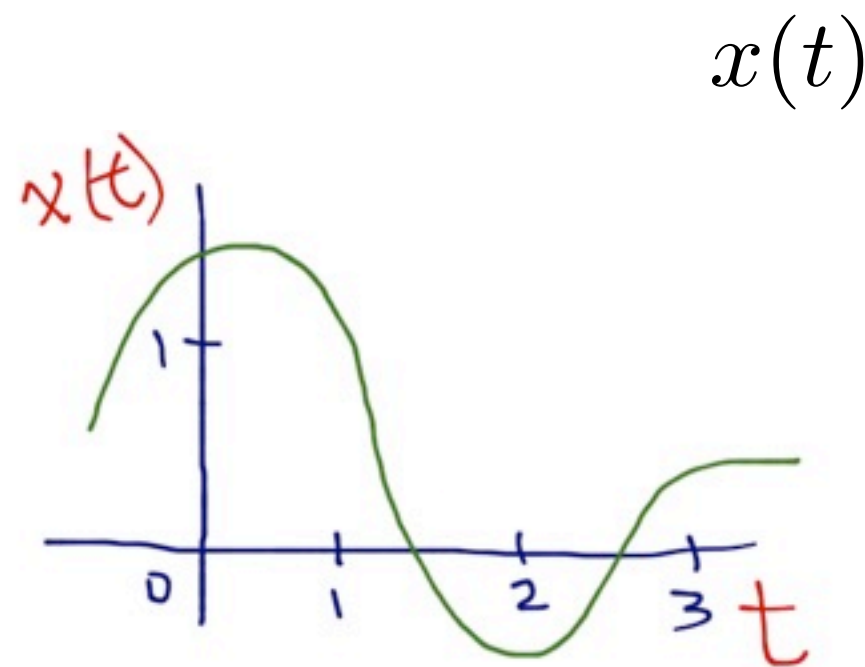
# Signals

- A “signal” describes how some physical quantity varies over time and/or space



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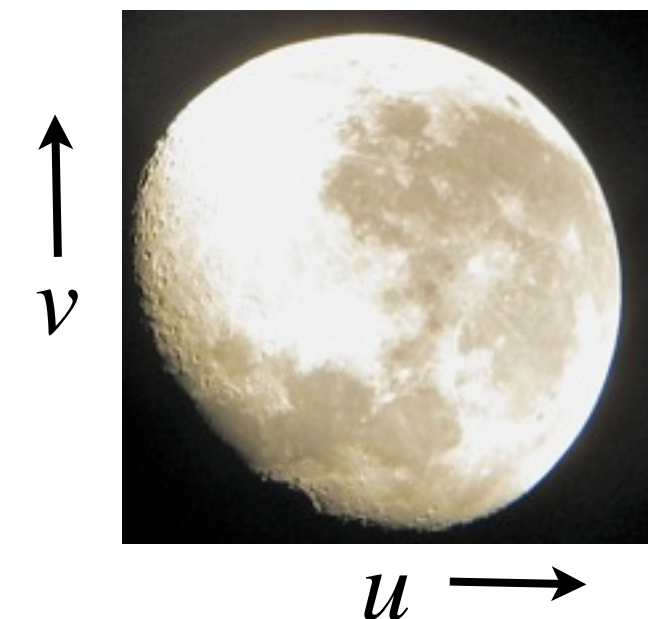
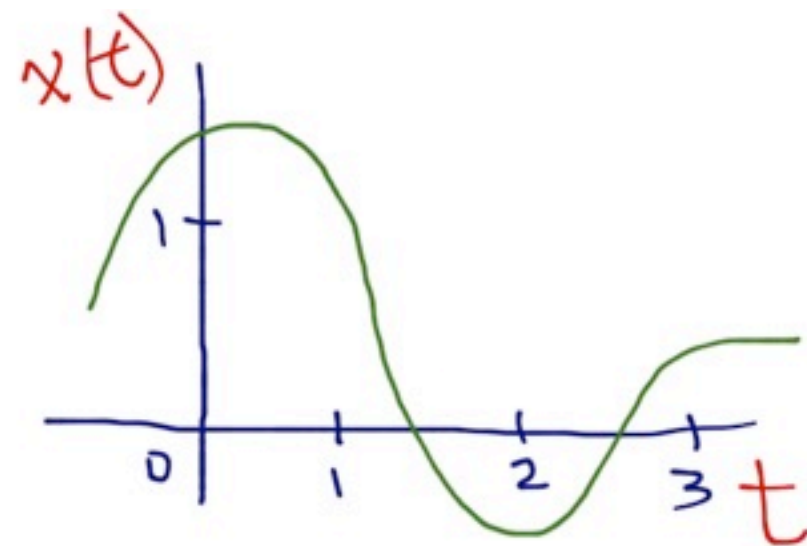
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- Mathematically: a function of one or more independent variables





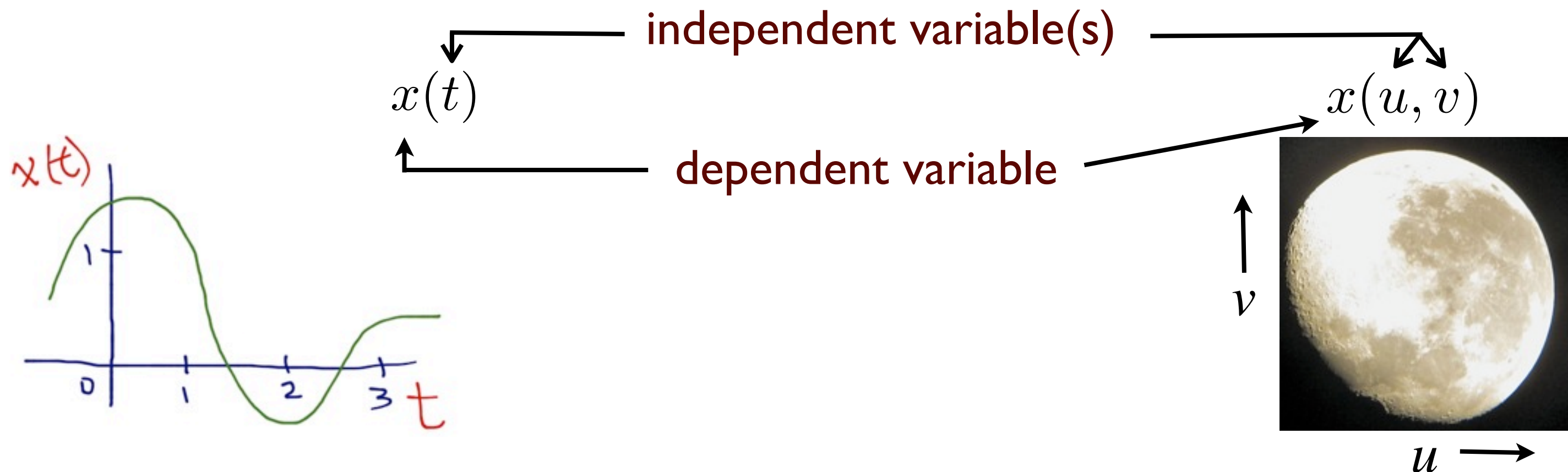
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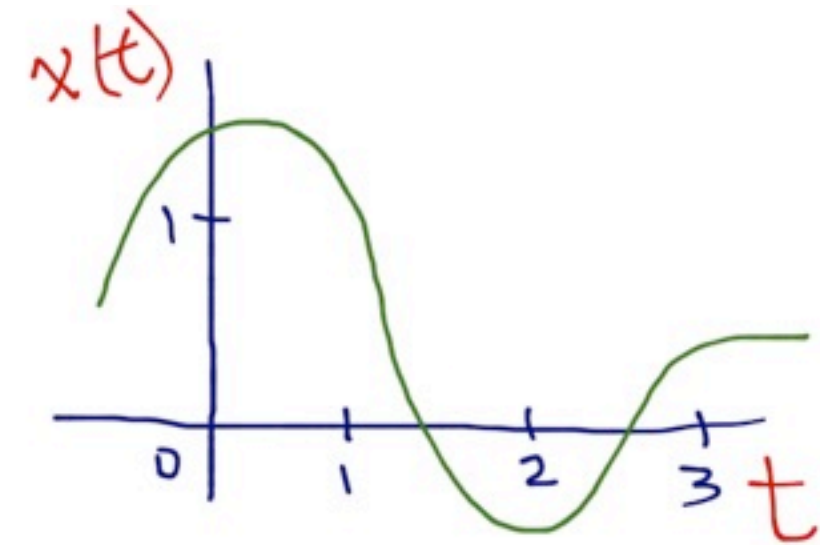
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# Continuous- and Discrete Indep Vbls

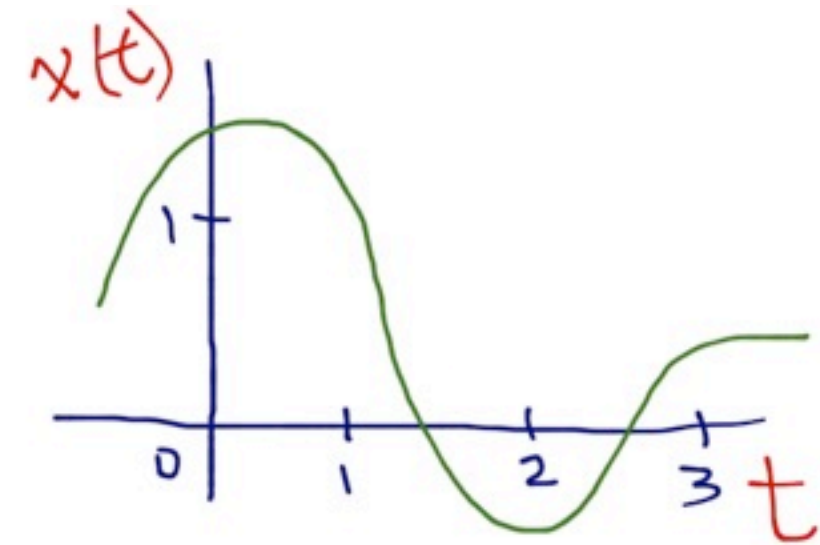
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# Continuous- and Discrete Indep Vbls

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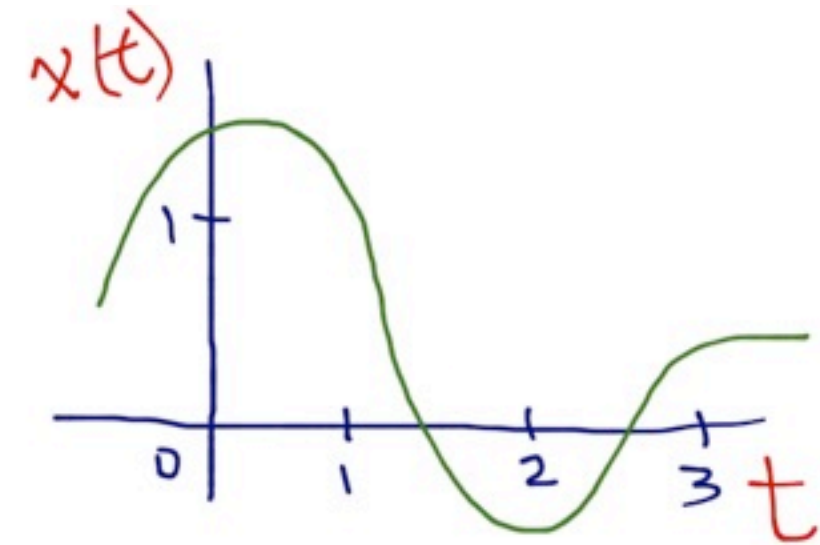
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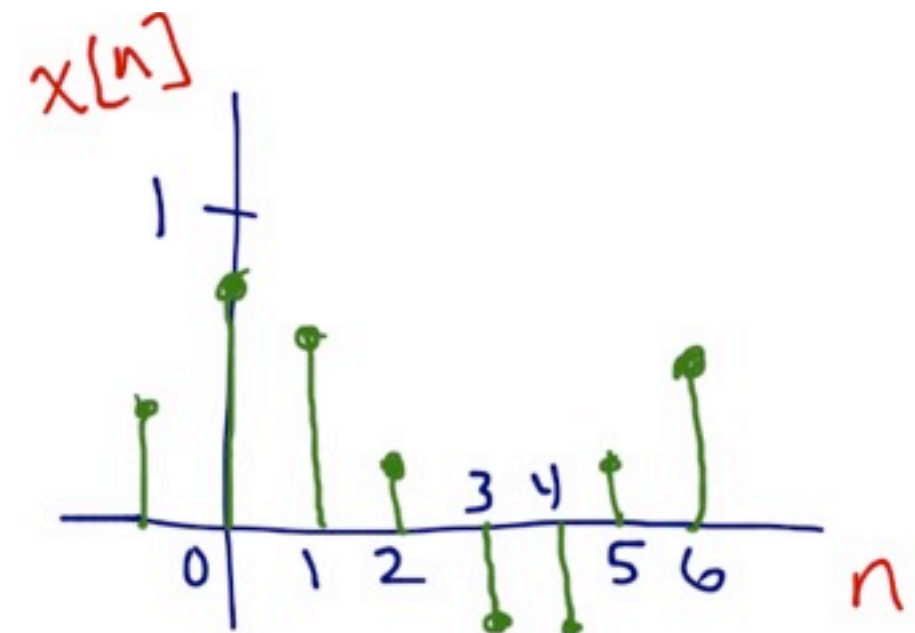
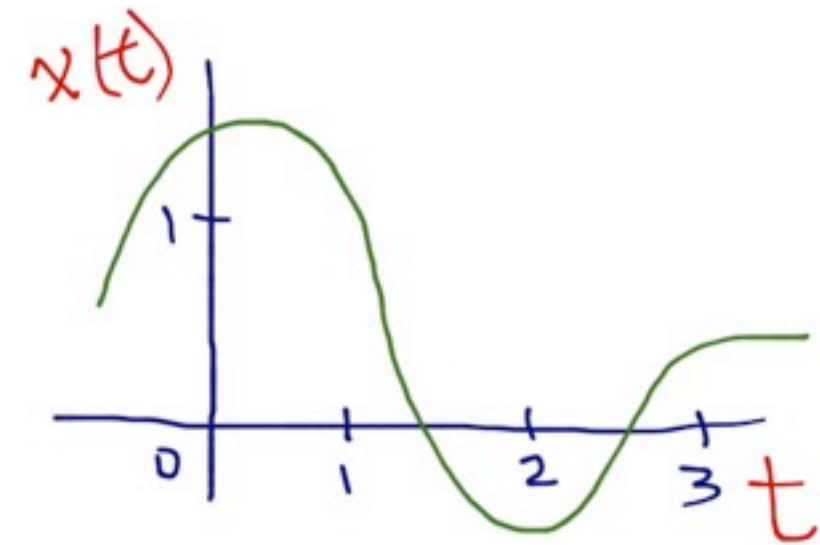


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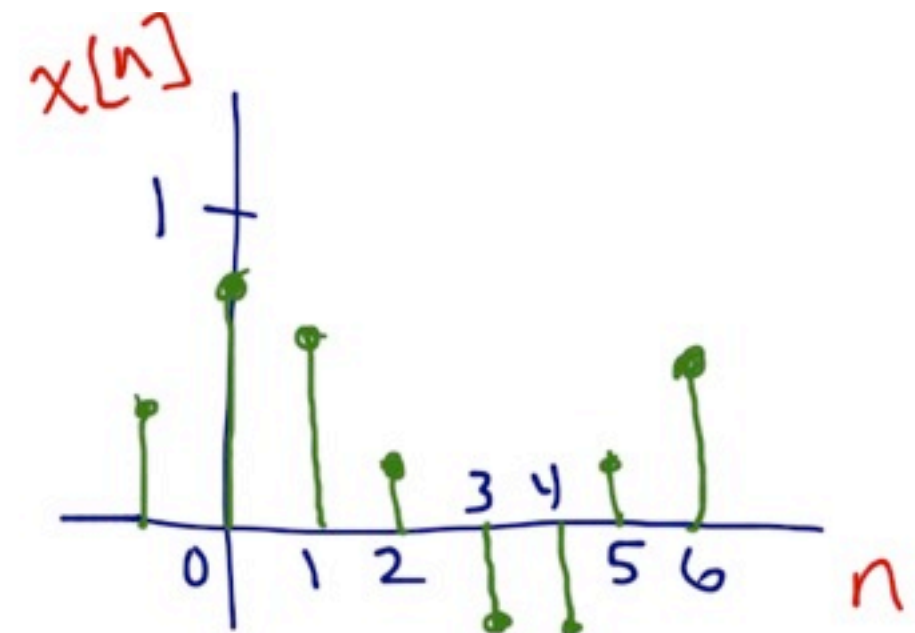
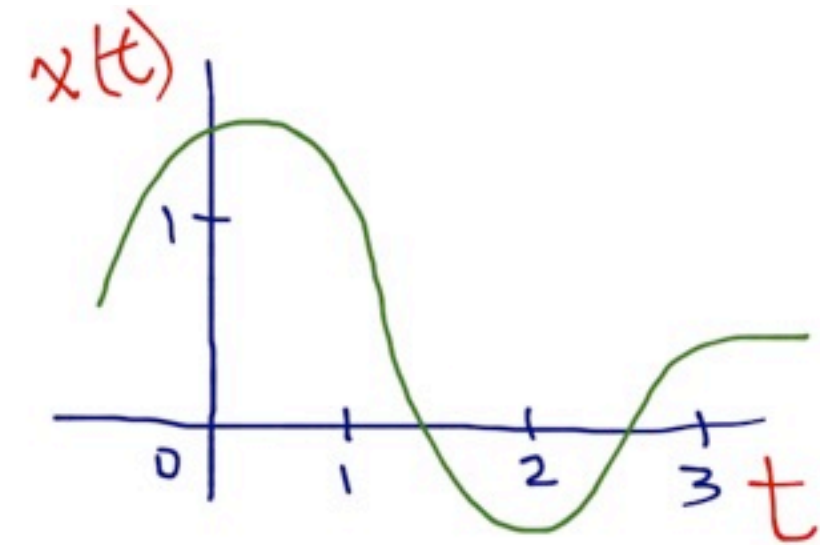


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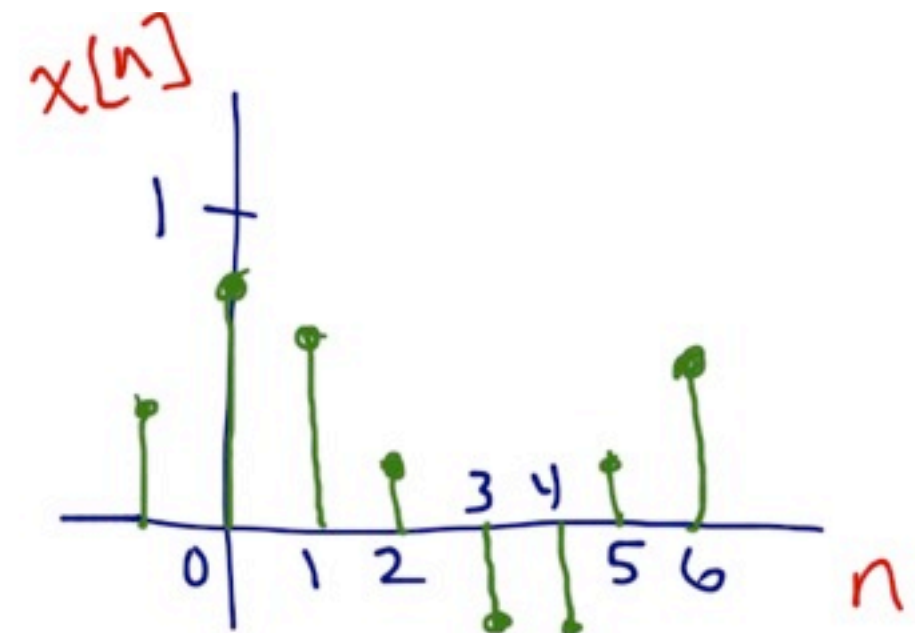
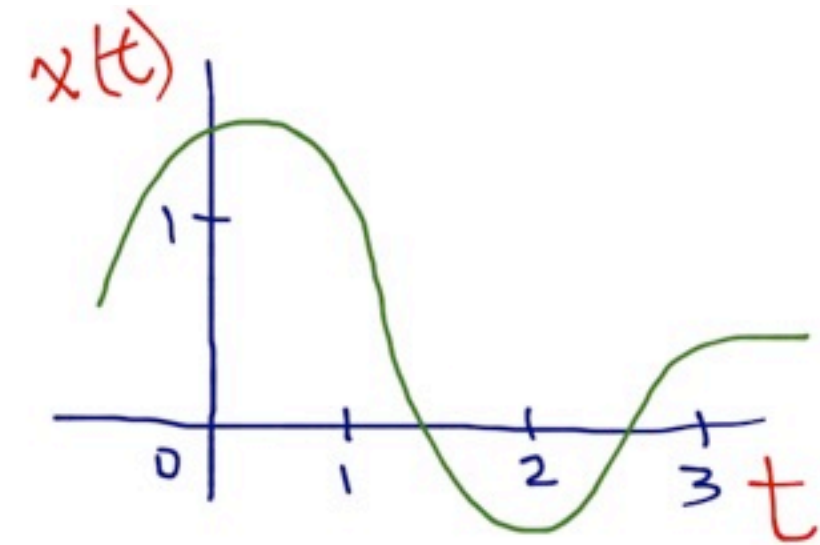


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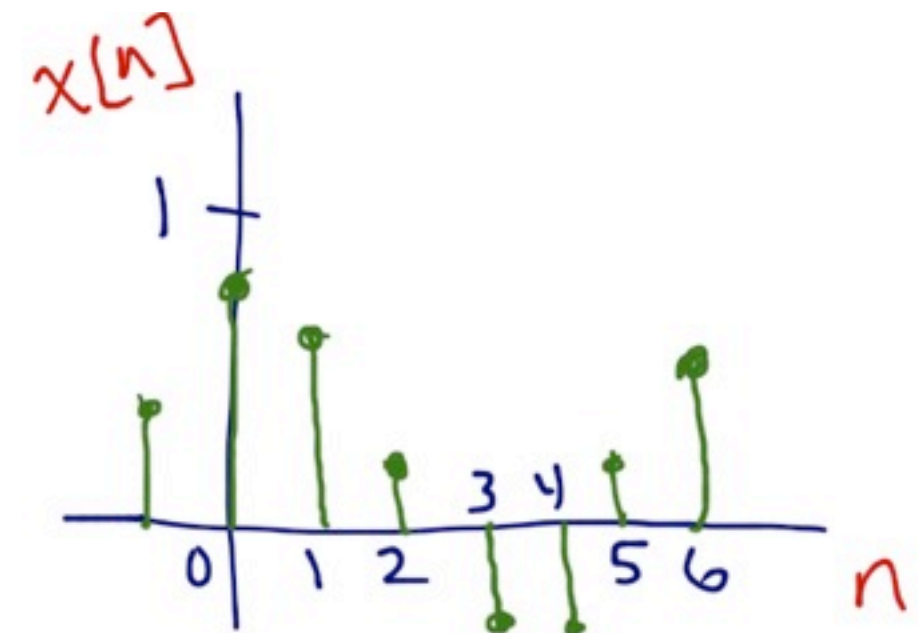
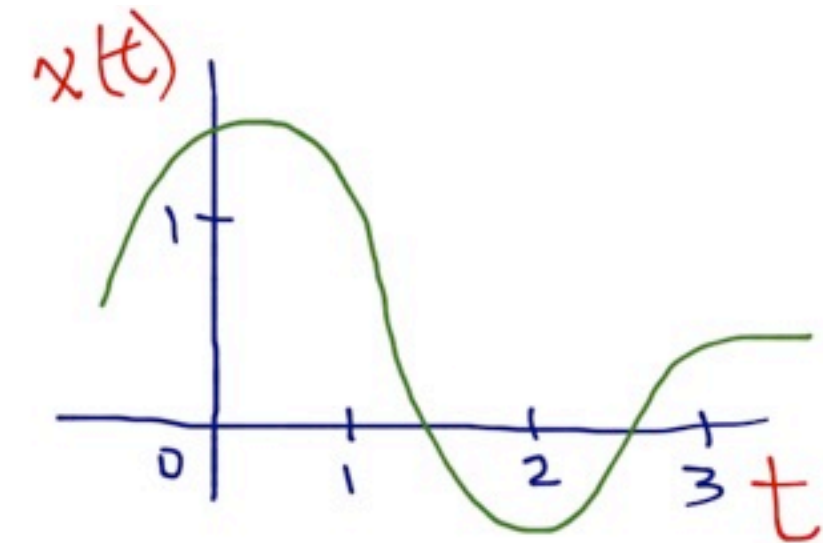


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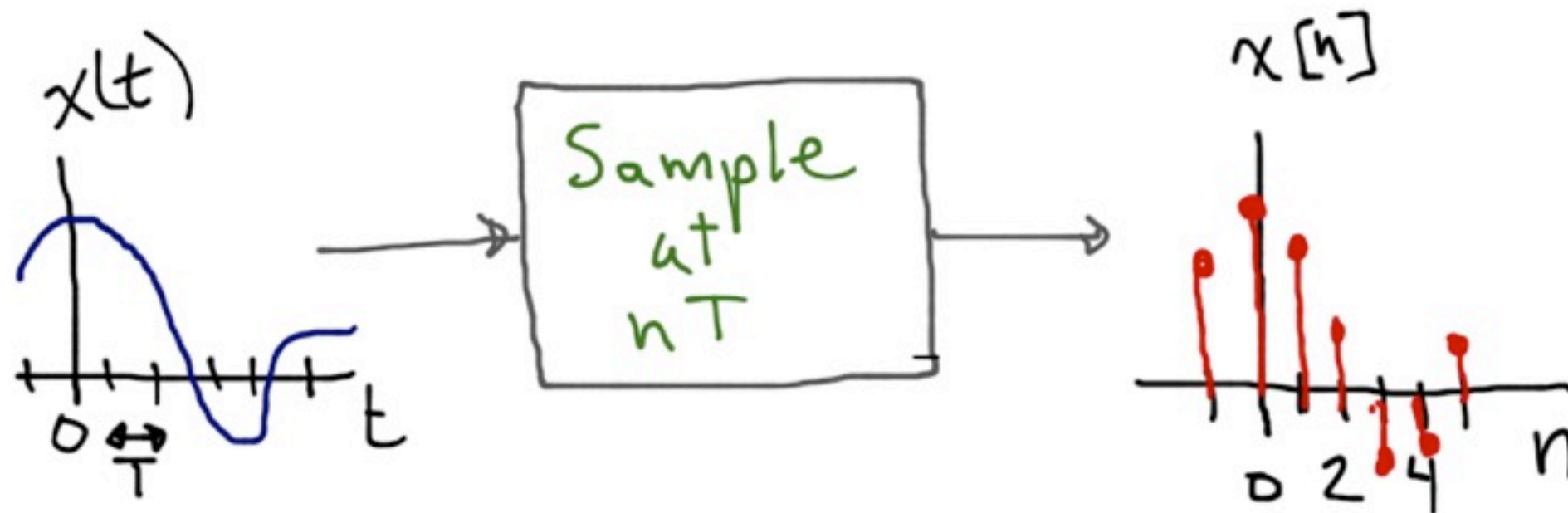
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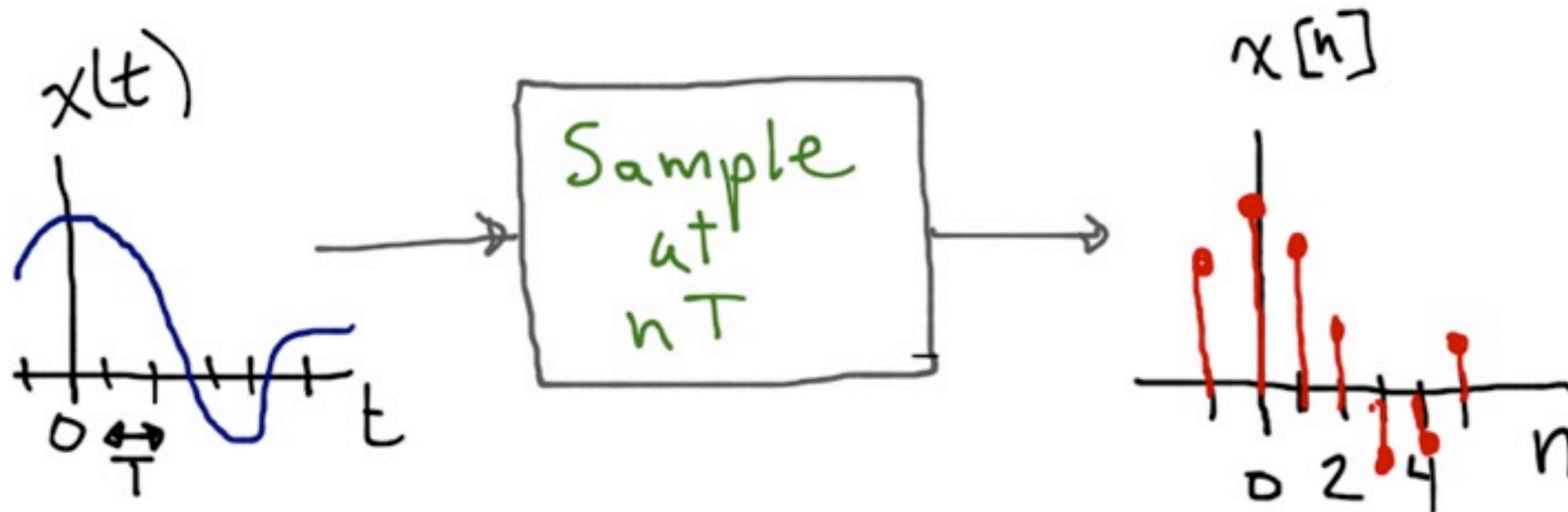
# Sampling



$$x[n] = x(t)|_{t=nT} = x(nT)$$

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- Often we obtain a discrete-time signal  $x[n]$  by sampling a continuous-time signal  $x(t)$

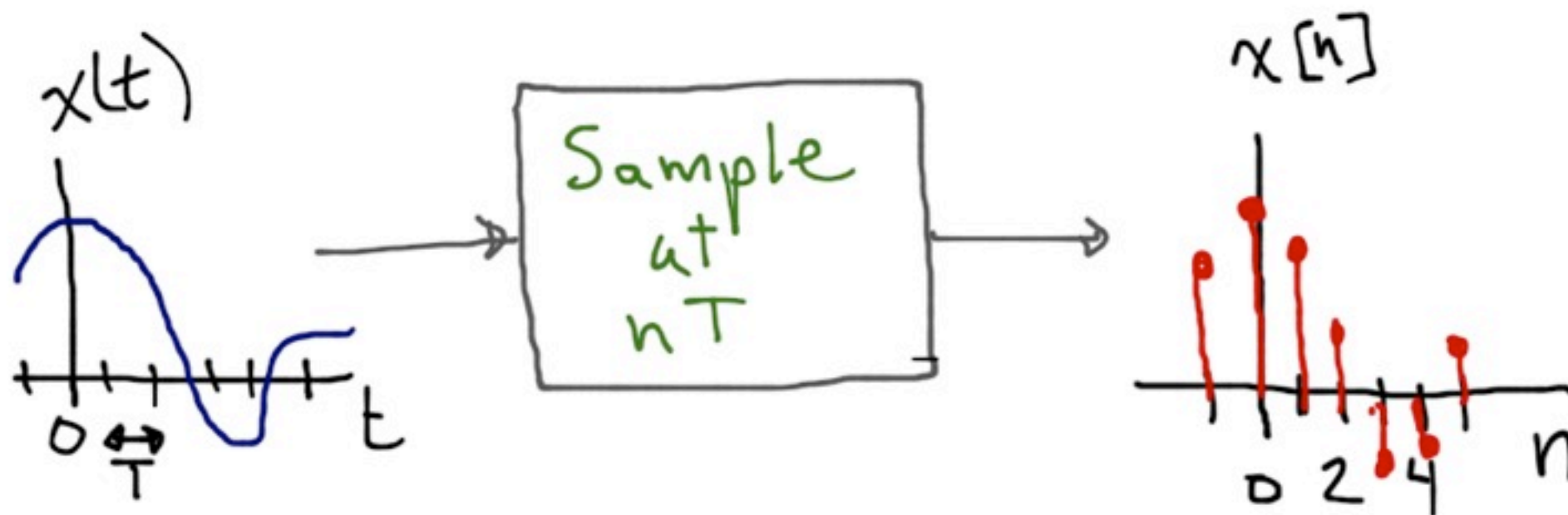


Examples

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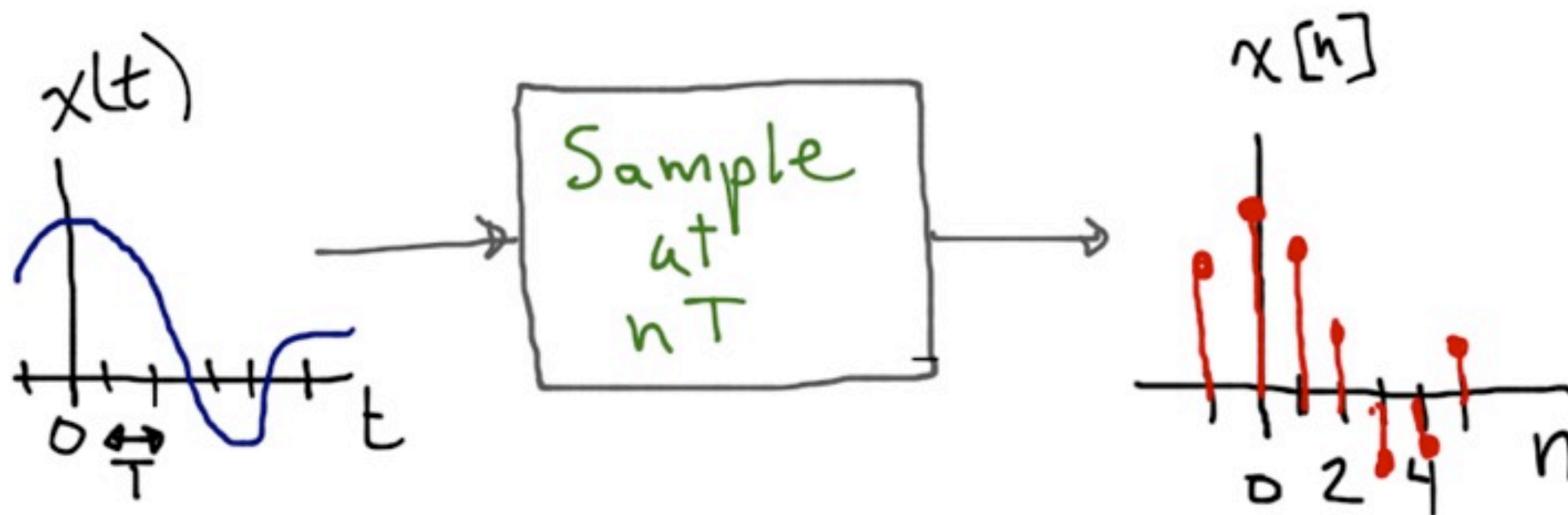
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## Examples

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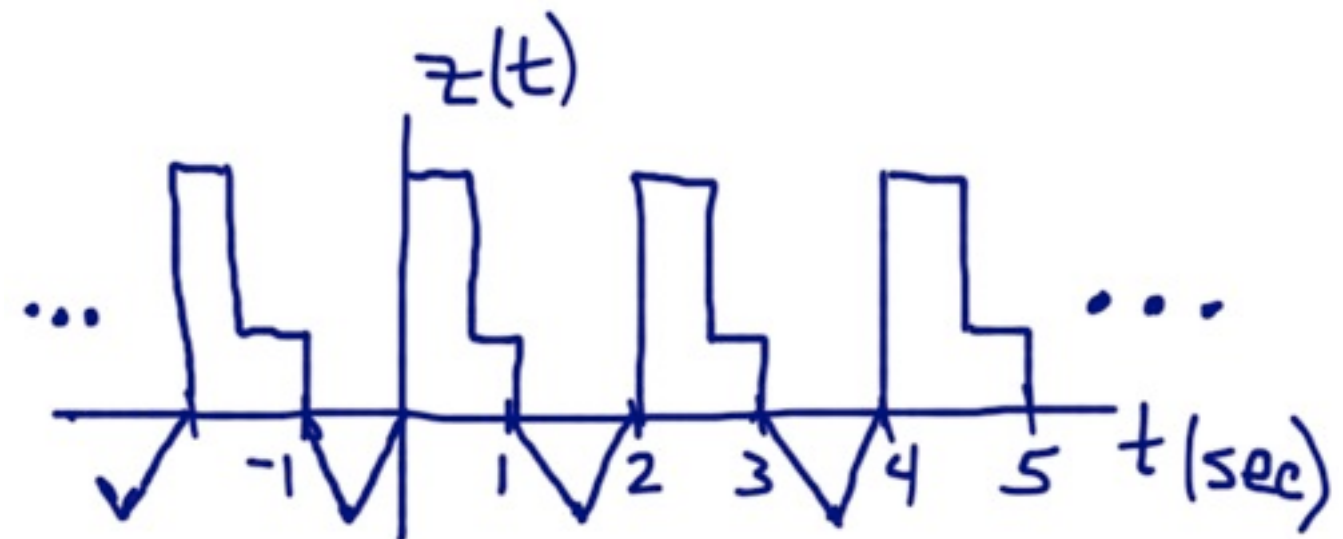
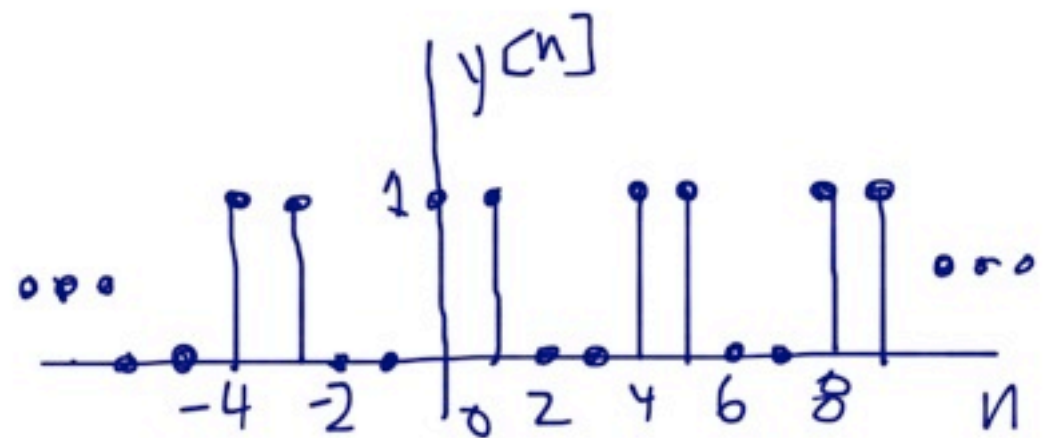
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- Signals stored in a computer must be discrete!
- Common to connect samples with straight lines
  - visual clarity with large numbers of samples
  - Use continuous time axis labels to visualize as continuous-time signal

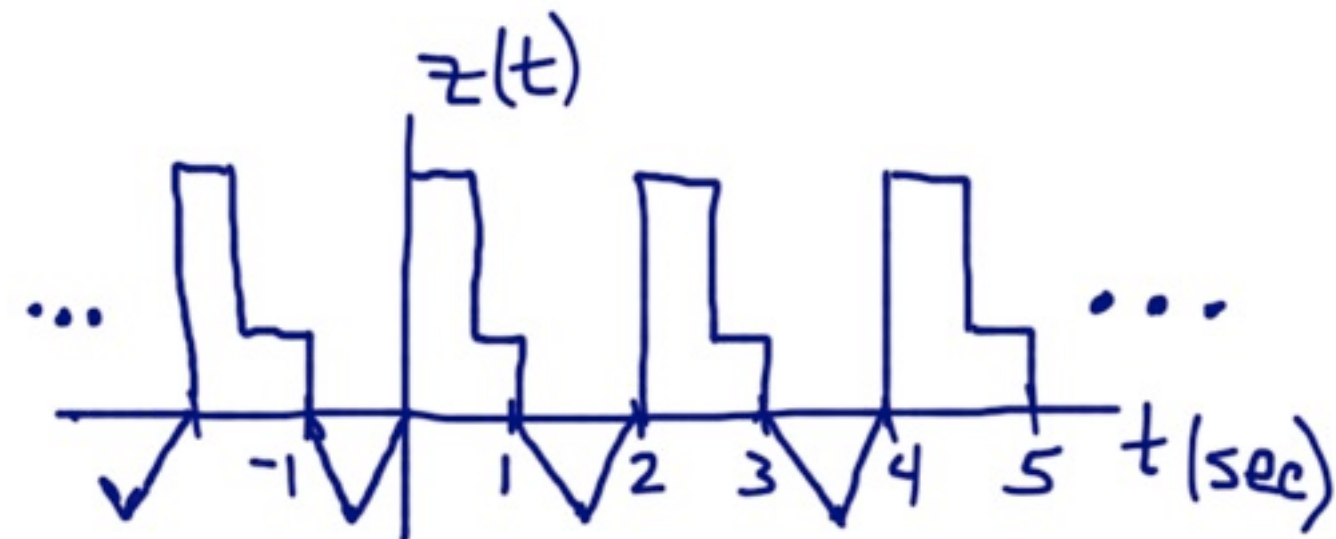
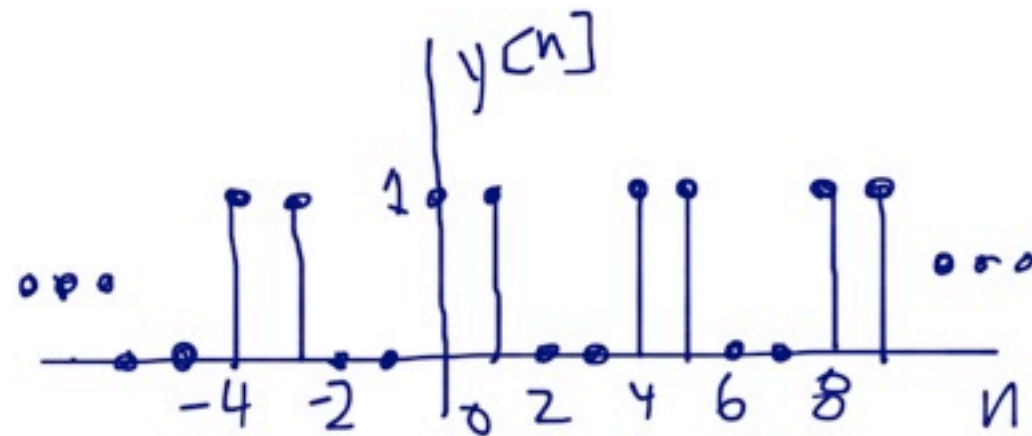
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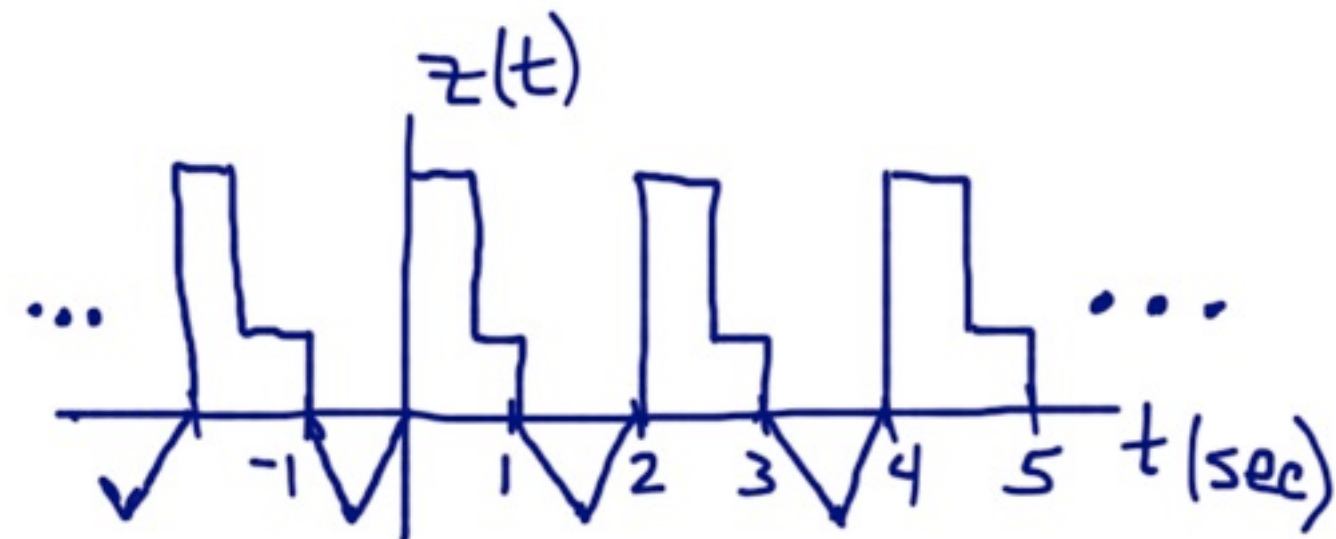
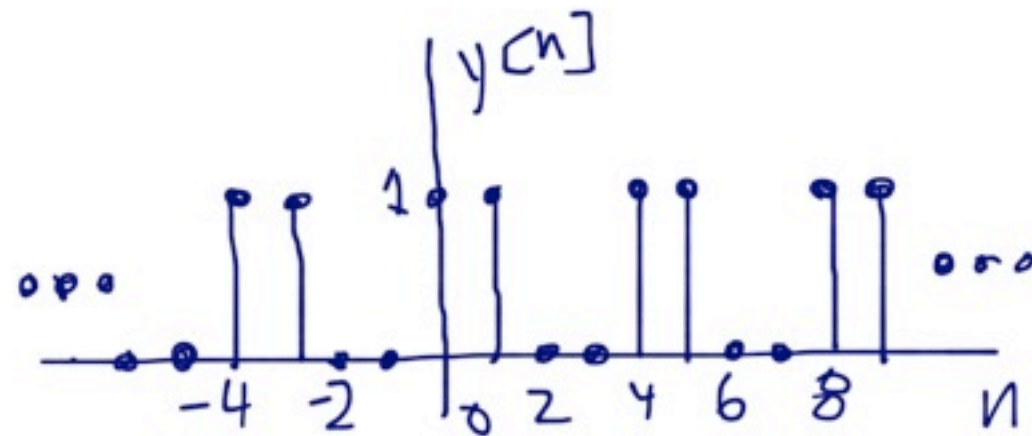
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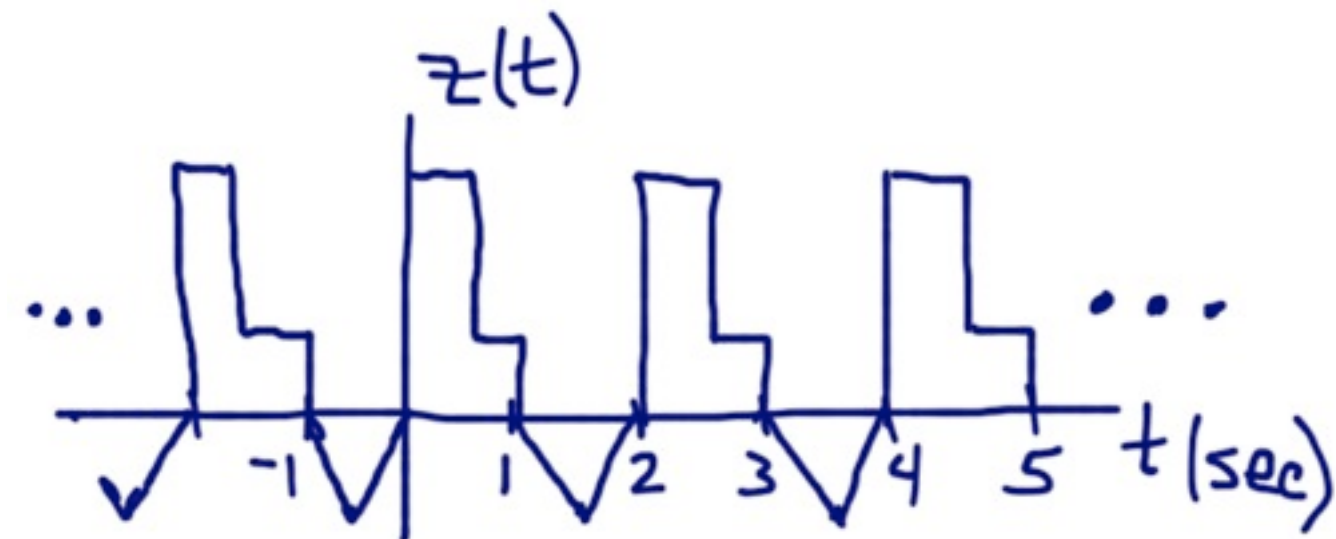
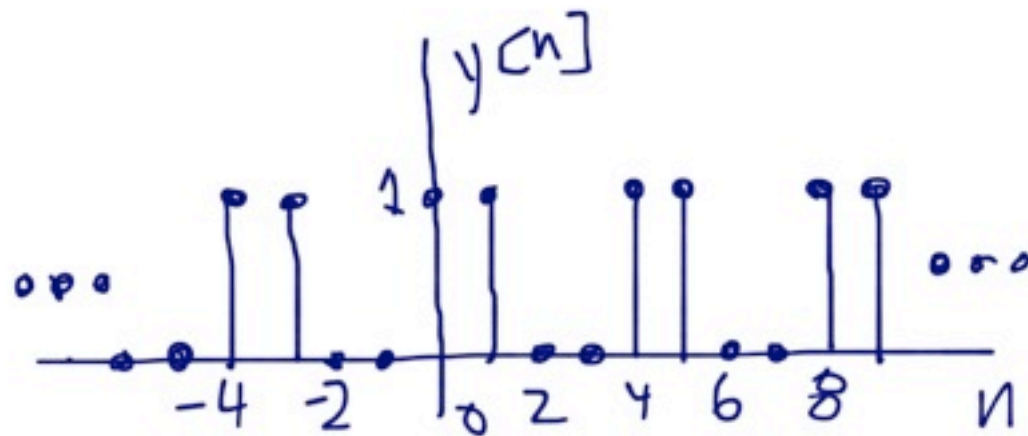
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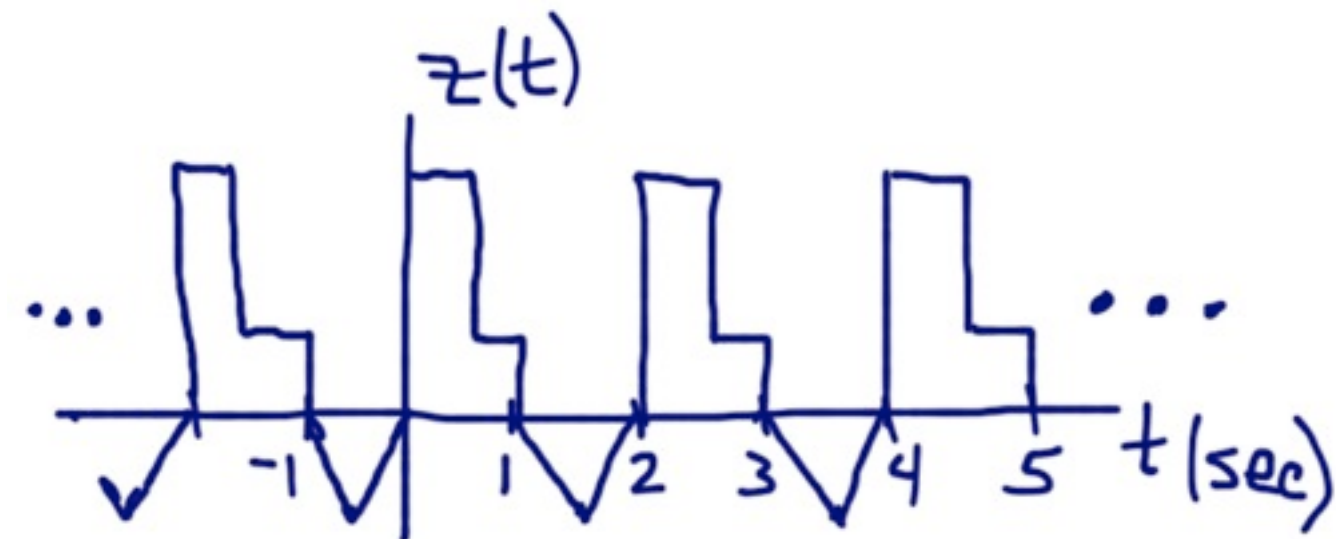
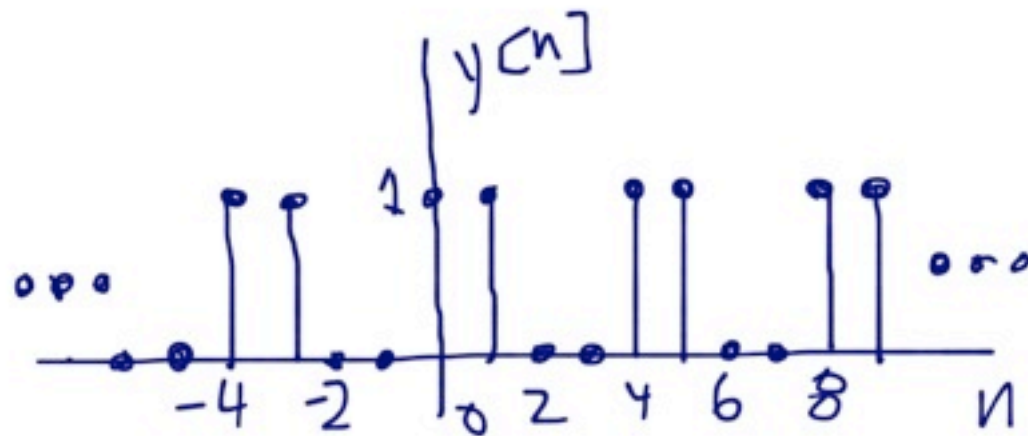
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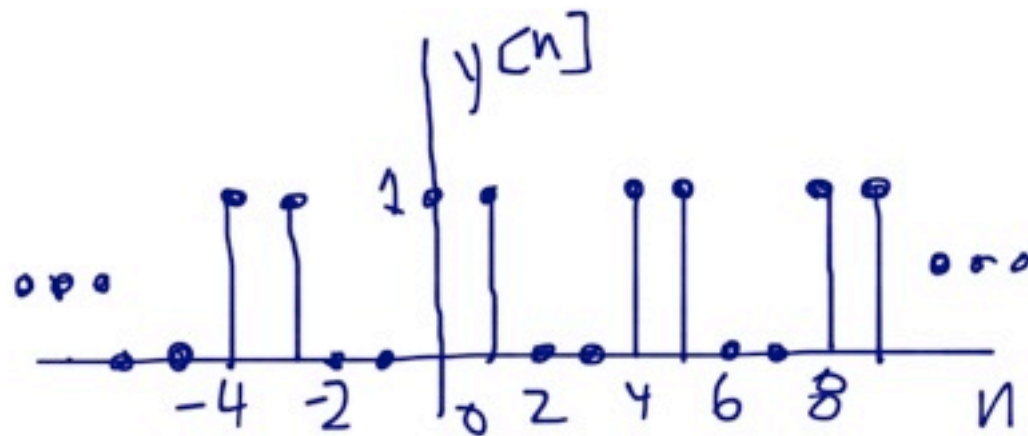
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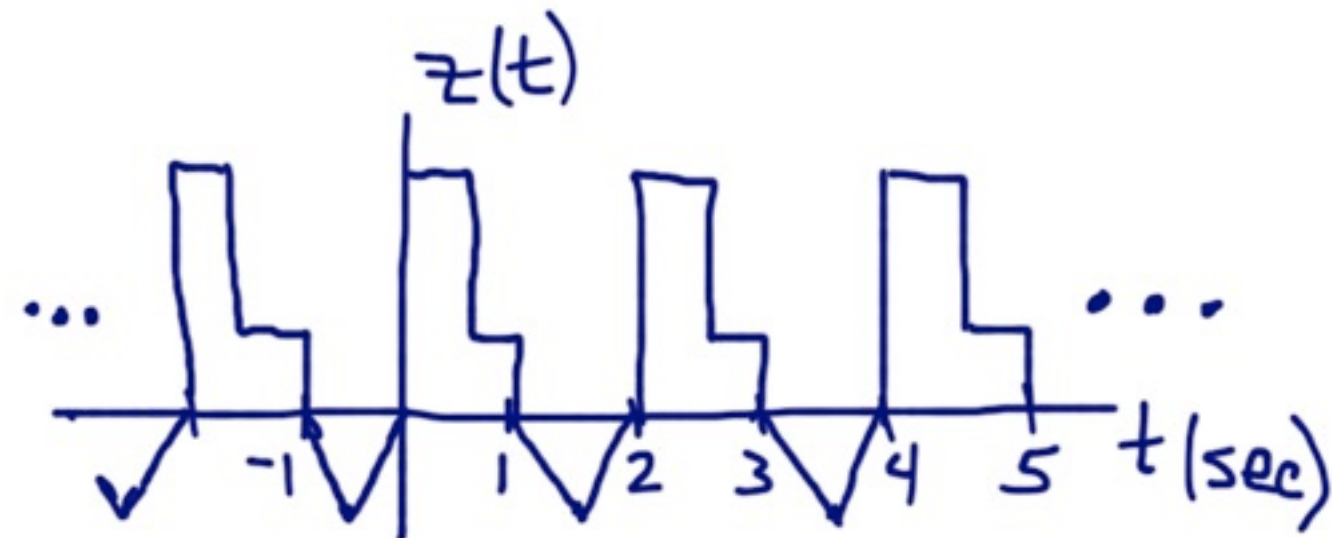
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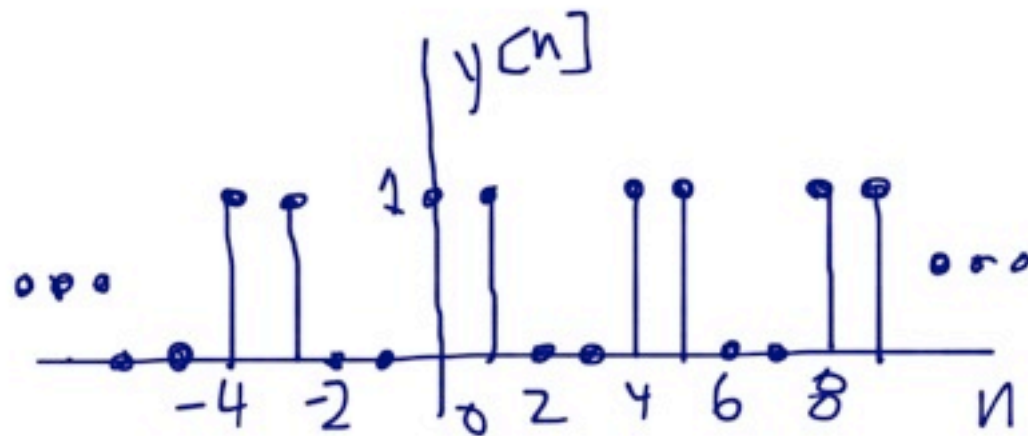
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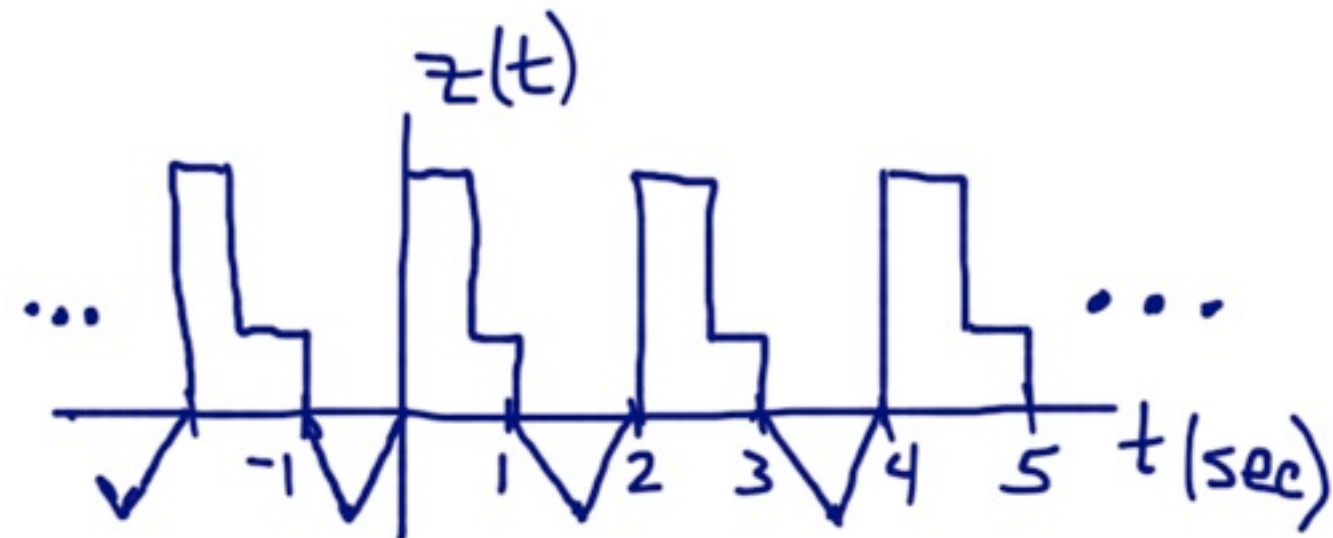
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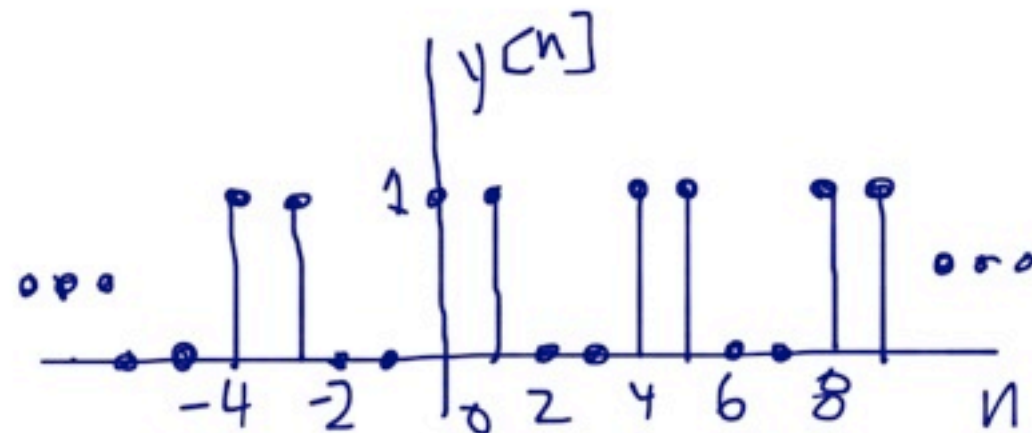
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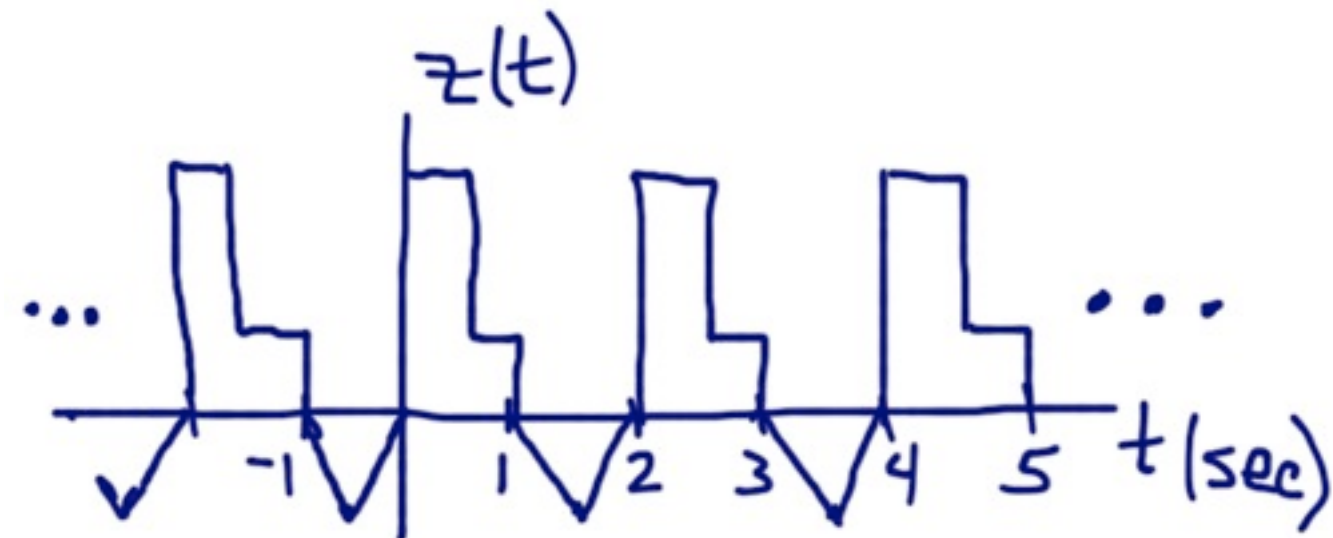
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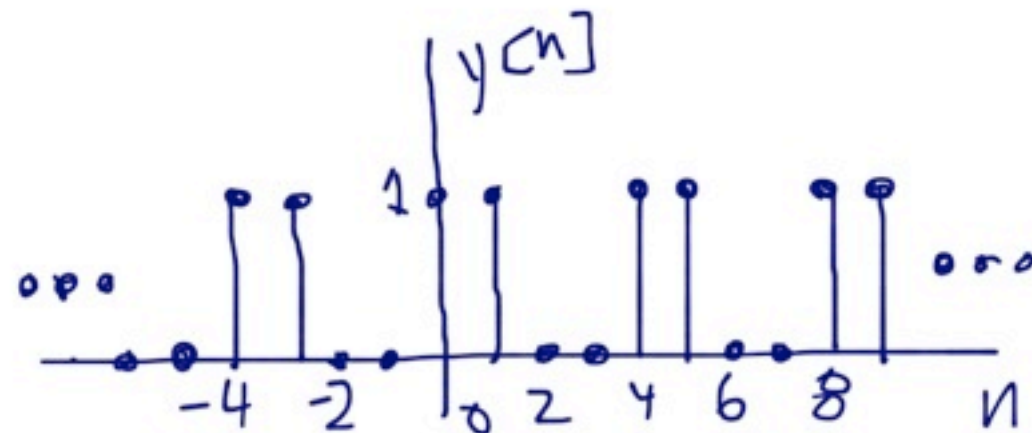
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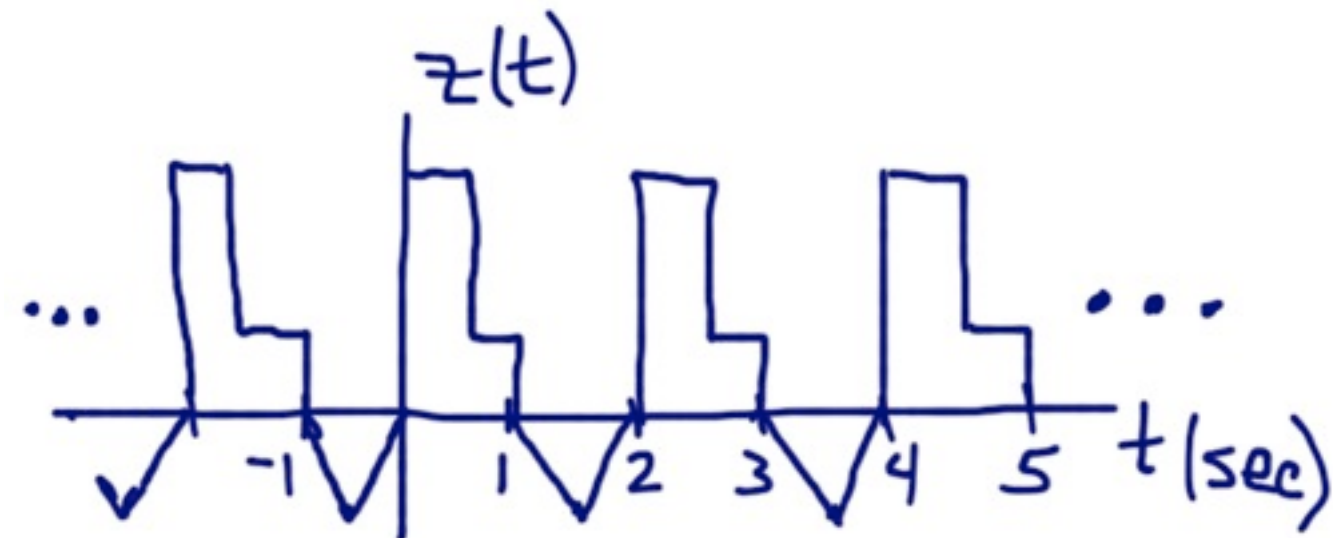
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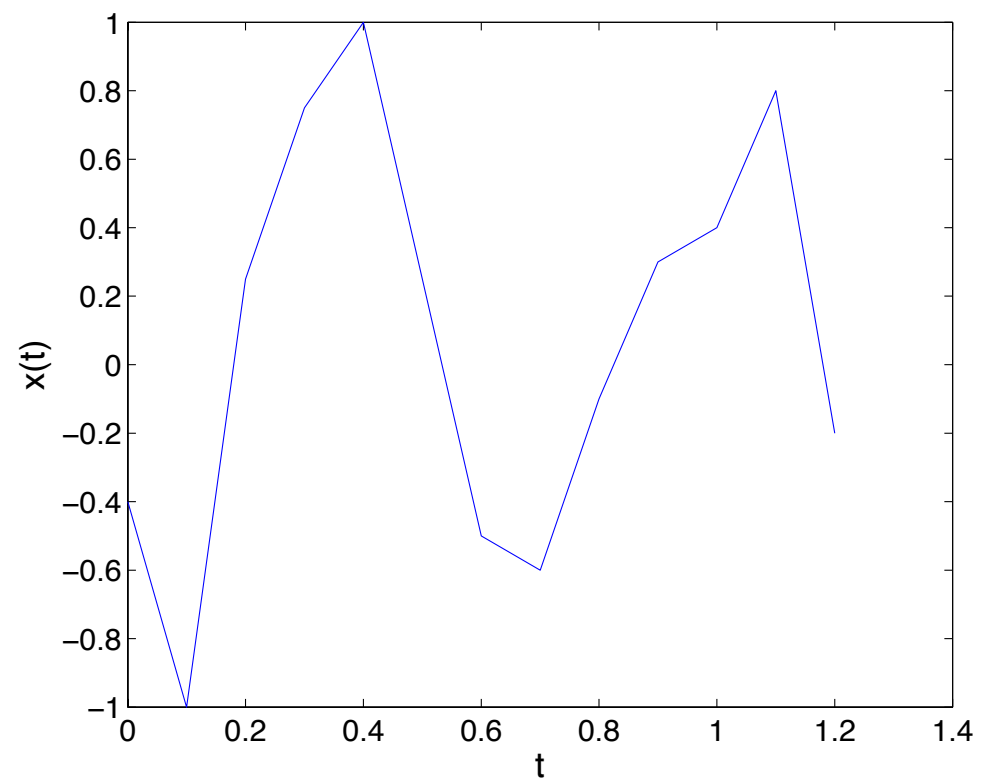
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- Brain electrical activity: “normal” vs seizure
- Speech
- Saxophone

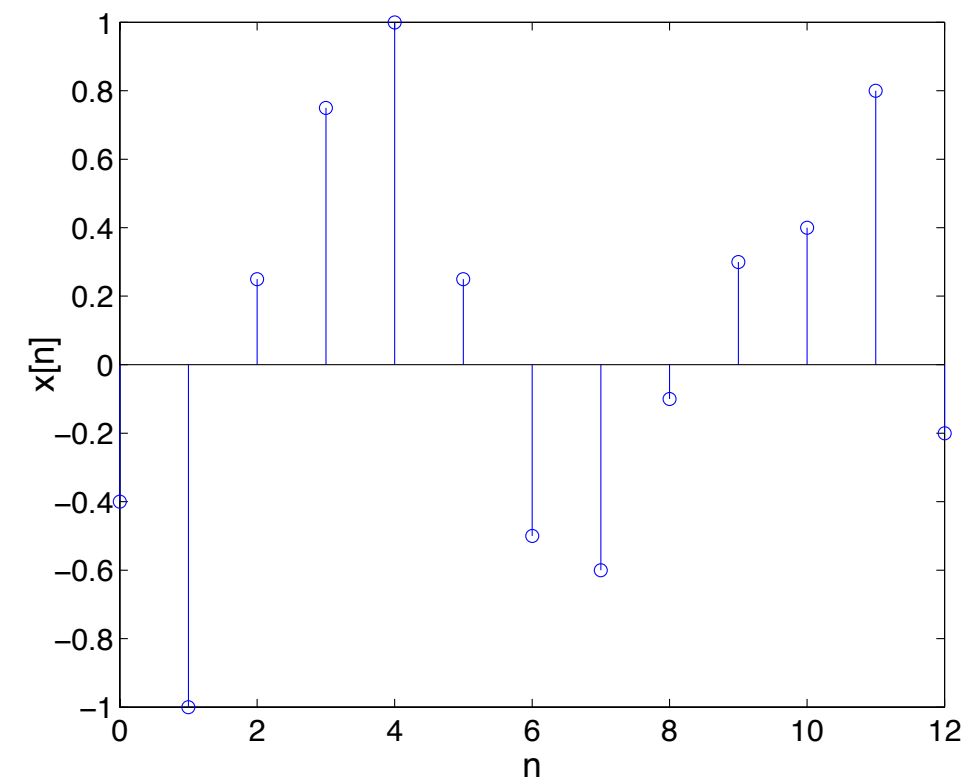
# Displaying Signals in MATLAB

```
x = [-0.4,-1,0.25,0.75,1,0.25,-0.5,-0.6,-0.1,0.3,0.4,0.8,-0.2];  
t = [0:12]*0.1;  
n = 0:12;
```

```
plot(t,x)  
xlabel('t')  
ylabel('x(t)')
```



```
stem(n,x)  
xlabel('n')  
ylabel('x[n]')
```





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- Independent variable can be continuous or discrete valued
- Periodicity – does a signal repeat – is an important property
- Practical definitions